## 1973-2023 INDEX of PROBLEMS & SOLUTIONS

VOLUMES 1-54.5

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## THE COLLEGE MATHEMATICS JOURNAL (Including the TWO YEAR COLLEGE MATHEMATICS JOURNAL)

prepared by

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## Notes:

1. All entries are in the format:

Problem Number.

Proposer, Volume.Issue Number(Year)Page of publication

**Topic of problem** as interpreted by the indexer

Solution Title determined by the Problem Editors Volume.Issue Number(Year)Page

- 2. The Two Year College Mathematics Journal began publishing in 1970, but the problem section did not begin until Volume 4 in 1973.
- 3. Please report any errors or omissions to the indexer at <charliecook29150@aim.com>.
- 4. \*\*\*\* indicates problems for which a Solution is pending.

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Solution: Convexity of  $(x + 1/x)^a$  12.1(1981)66

150.

Proposer: Aron Pinker 10.4(1979)294

Topic: Ccan a determinant with positive entries be zero? Solution: Invertibility of matrices in Q|M| 12.1(1981)67

151.

Proposer: Peter A. Lindstrom 10.5(1979)359

Topic: Equality of integrals from 1 to x and from y to xy

Solution: The g that solves  $\int_1^x g(t)dt = \int_y^{xy} g(t)dt$  12.2(1981)155

152.

Proposer: Daniel Gallin 10.5(1979)359

Topic: Best lower bound for the probability of n events

Solution: Probability of simultaneously occurring events 12.2(1981)157

153.

Proposer: K. R. S. Sastry 10.5(1979)359

Topic: Determining the area of a given parallelogram Solution: Squaring a parallelogram 12.2(1981)158

154.

Proposer: V. N. Murty 10.5(1979)360

Topic: Inequality using 4 real numbers whose determinant is 1 Solution: Inequality for triangles and for trace *AB* 12.2(1981)159

155.

Proposer: Norman Schaumberger 10.5(1979)360

Topic: Finding the limit of the mean of *n* elements whose product is 1

Solution: Distinct elements with equal means 12.2(1981)162

Proposer: Aron Pinkin 11.1(1980)61

Topic: Product inequality and area identity of triangles constructed within a given triangle

Solution: Harmonic division of real coordinates 12.3(1981)213

157.

Proposer: Warren Page 11.1(1980)61; Corrected 11.4(1980)275 Topic: Inequality relating to 2 sequences of positive real numbers

Solution: The inequality  $(1/n \Sigma (y_i - y_{avg})^2)^{1/2} < 1/2 (max y_i - min y_i) 12.3(1981)214$ 

158.

Proposer: V. N. Murty & J.M. Maynard 11.1(1980)61 Topic: 2 variable inequality for positive numbers

Solution: It's a sinh 12.3(1981)215

159.

Proposer: Norman Schaumberger 11.1(1980)62

Topic: Evaluating a sum of arctangents of reciprocal quantities Solution: Generalization of  $\tan^{-1}(\frac{1}{2}) + \tan^{-1}(\frac{1}{3}) = \pi/4$  12.3(1981)216

160.

Proposer: R. S. Luthar 11.1(1980)62

Topic: N&S condition on sums of sines of angles of 2 triangles inscribed in a circle

Solution: Inscribed triangles revisited 12.3(1981)218

161.

Proposer: Michael W. Ecker 11.2(1980)131

Topic: Existence of a nonzero row-skew-symmetric matrix Solution: Row-skew symmetric matrices 12.4(1981)275

162.

Proposer: Walter Bluger 11.2(1980)131

Topic: Finding the minimum number acute triangles which partition a square

Solution: Acute minimal triangulation of a square 12.4(1981)276

163.

Proposer: Wm. R. Klinger 11.2(1980)131; Corrected 12.2(1981)154 Topic: Summation inequalities determined from a finite sequence

Solution: The inequality  $\Sigma (\Sigma a^r / \Sigma a^s) \Sigma a^{r-s} = 13.1(1992)66$ 

164.

Proposer: V. N. Murty 11.2(1980)132

Topic: Evaluating a definite logarithmic integral

Solution: Calculation of  $\int_0^1 (\ln x) \ln(1-x) dx$  12.4(1981)277

165.

Proposer: Bertram Kabak & Norman Schaumberger 11.2(1980)132

Topic: Inequalities relating to distances between interior points of a triangle

Solution: Inequalities for interior points of a triangle 12.5(1981)337

Proposer: V. N. Murty 11.3(1980)208

Topic: Establishing some algebraic - exponential inequalities

Solution: Polynomial bounds for a meromorphic function 12.5(1981)339

167.

Proposer: Michael W. Ecker 11.3(1980)208

Topic: Truth values of statements concerning numbers in a list Solution: Truth values for self-descriptive sentences 12.5(1981)343

168.

Proposer: Anonymous 11.3(1980)209

Topic: Finding a unique Solution to the equation,  $a^x = x^n$  for a > 0

Solution: Unique Solution of  $a^x = x^n$  12.5(1981)343

169.

Proposer: Alan Wayne 11.3(1980)209

Topic: Find an integer whose square has consecutive digits whose product is divisible by 7

Solution: N<sup>2</sup> terminating in 7N 12.5(1981)344

170.

Proposer: Sidney Penner 11.3(1980)209

Topic: Delete the minimum number of squares from a checkerboard leaving a unique

configuration of remaining squares

Solution: Uniquely modified checkerboard 12.5(1981)345

171.

Proposer: Thoms E. Elsner 11.4(1980)275

Topic: Inequalities involving a canted washer with an internal centroid

Solution: Centroid of canted washer 13.1(1982)67

172.

Proposer: V. N. Murty 11.4(1980)276

Topic: Establishing sums of convergent sequences minus their limits

Solution: The series  $\Sigma_{i=1} \Sigma_{k=i+1} (-1)^k / (km + b) = 13.1(1982)67$ 

173.

Proposer: Lance Littlejohn 11.4(1980)276

Topic: Proving that an upper triangular matrix is nilpotent

Solution: Powers of a triangular matrix 13.1(1982)69

174.

Proposer: Alan Wayne 11.4(1980)276

Topic: Solve a fifth degree polynomial equation

Solution: Cyclic quintic 13.1(1982)70

175.

Proposer: Norman Schaumberger 11.4(1980)276

Topic: Necessary & sufficient condition that a certain triangle is equilateral

Solution: Condition for equilateral triangles 13.1(1982)71

Proposer: Michael W. Ecker 11.5(1980)336

Topic: Evaluate the determinant of a given matrix Solution: Determinant of (poly(i,j)) 13.2(1982)148

177.

Proposer: Alvin J. Paullay & Sidney Penner 11.5(1980)336

Topic: Show that a triangular 2-colored array of pennies has 3 of the same color whose

centers form an equilateral triangle

Solution: Array of head-and-tail discs 13.2(1982)150

178.

Proposer: Roger L. Creech 11.5(1980)336

Topic: Probability that a segment inside a circle is shorter that the radius

Solution: Probability of a subradial distance 13.2(1982)151

179.

Proposer: Alan Wayne 11.5(1980)336

Topic: Alphanumeric puzzles

Solution: Two division cryptarithms 13.2(1982)152

180.

Proposer: V. N. Murty 11.5(1980)336

Topic: Solving a bracket function equation

Solution: Greatest integer function identity 13.2(1982)153

181.

Proposer: Thomas E. Moore 12.1(1981)63

Topic: Prove that a Fermat number is not a product of 2 Mersenne numbers

Solution: Can a Fermat number be a Mersenne product? 13.3(1982)208

182.

Proposer: Martin Berman 12.1(1981)63

Topic: Determine the expected number of inversions in a set of counters

Solution: Expected number of inversions 13.3(1982)208

183.

Proposer: Milton P. Eisner 12.1(1981)63

Topic: Necessary & sufficient condition for triples in arithmetic progressions

Solution: Casting out arithmetic triples 13.3(1982)209

184.

Proposer: J. L. Brenner 12.1(1981)64

Topic: Proving or disproving trigonometric inequalities Solution: Trigonometric implication 13.3(1982)210

185.

Proposer: Norman Schaumberger 12.1(1981)64

Topic: Finding rational Solutions of an algebraic equation Solution: Rational Solutions of  $x^{x+y} = (x+y)^y$  13.3(1982)212

Proposer: Stewart M. Venit 12.2(1981)155

Topic: A unique square matrix of any size having 3 given properties

Solution: \*\*\*\*\*

187.

Proposer: Norman Schaumberger 12.2(1981)155

Topic: Find the side of an equilateral triangle from distances from a fixed point to vertices

Solution: Distance to a vertex to an equilateral triangle 13.4(1982)278

188.

Proposer: Sidney Kravitz 12.2(1981)155

Topic: Calculating quantities using a fixed number of keystrokes on a calculator

Solution: Alternatives on a hand held calculator 13.4(1982)282

189.

Proposer: Charles W. Trigg 12.2(1981)155

Topic: 4-term arithmetic progressions of 3-digit primes

Solution: Arithmetic progression of primes with permuted digits 13.5(1982)334

190.

Proposer: Zalman Usiskin 12.2(1981)155

Topic: Solving a trig equation of tangent functions

Solution: Tangent product 13.5(1982)335

191.

Proposer: Michael Ecker 12.3(1981)212

Topic: Approximated rational fractions by decimals

Solution: Arithmetical errors of the types 1/a = a and a/b = ab 13.5(1982)336

192.

Proposer: V. N. Murty 12.3(1981)213

Topic: Limit of the n<sup>th</sup> root of the geometric mean of binomial coefficients

Solution: Geometric mean of binomial coefficients 13.5(1982)337

193.

Proposer: K. R. S. Sastry 12.3(1981)213

Topic: Equations involving the inradius and circumradius of a triangle Solution: Inversion of a circle in a circle through its center 13.5(1982)339

194.

Proposer: Norman Schaumberger 12.3(1981)213

Topic: Inequality involving e and  $\pi$  Solution: Is  $(\pi^{\pi} e^{e})^{\frac{1}{2}}$  13.5(1982)340

195.

Proposer: Barney Bissinger 12.3(1981)213

Topic: Solving a trig equation of tangent functions Solution: Tan x = tan 2x tan 3x tan 4x 13.5(1982)341

Proposer: Kenneth Fogarty 12.4(1981)275

Topic: Can a non-median angle bisector in a triangle contain the centroid?

Solution: Envelope of lines bisecting a triangle 14.1(1983)65

197.

Proposer: Thomas E. Elsner 12.4(1981)275

Topic: Number of square matrices satisfying 3 conditions

Solution: Minimal matrices with vanishing adjoint 14.1(1983)68;

Rock bottom 15.4(1984)347

198.

Proposer: Aron Pinker & John Biggs 12.4(1981)275

Topic: Equality involving internal segments in a right triangle

Solution: Nested right triangles 14.1(1983)69

199.

Proposer: F. David Hammer 12.4(1981)275

Topic: Possible identity of a sum of polynomial quantities times a binomial coefficient

Solution: Nth difference of a polynomial 14.1(1983)69

200.

Proposer: Chris Jantzen 12.4(1981)275

Topic: Number of dice needed to maximize the probability of rolling n 6's in one toss

Solution: Optimal number of Ttials in a binomial experiment 14.1(1983)70

201.

Proposer: Norman Schaumberger 12.5(1981)336

Topic: A series of inequalities involving reciprocals of cubic integers

Solution: Eliminating the remainder of a series 15.3(1984)267

202.

Proposer: V. N. Murty 12.5(1981)336

Topic: Inequality involvint the mean and variance of 2 subsets of real numbers

Solution: \*\*\*\*\*

203.

Proposer: Alan Wayne 12.5(1981)337

Topic: Finding optimal regular polygons inscribed in a larger regular polygon

Solution: \*\*\*\*\*

204.

Proposer: Norman L. Swanson 12.5(1981)337

Topic: Solving for integers that satisfy a factorial equation Solution: What is strange About 6!7!=10!? 14.2(1983)173

205.

Proposer: Jerry Metzger 12.5(1981)337

Topic: Finding the path of a dog chasing a rabbit

Solution: The path of a dog pursuing a rabbit 14.2(1983)174

Proposer: Stewart M. Venit 13.1(1982)64

Topic: Finding eigenvalues of one matrix and verifying properties of another

Solution: Matrix medley 14.2(1983)176

207.

Proposer: Milton H. Hoehn 13.1(1982)65 Topic: Evaluating a sum of squared cosines

Solution:  $\Sigma \cos^2 \{(2k-1)\pi/2n\} = n/4 + 14.2(1983)178$ 

208.

Proposer: M. S. Klamkin 13.1(1982)65

Topic: Explain why the sum of 2 roots of a given quartic equation is 4

Solution: Depression of a biquadratic given the sum of two roots 14.3(1983)261

209.

Proposer: Aron Pinker 13.1(1982)65

Topic: Proving algebraic-logarithmic inequalities Solution: The logarithmic mean 14.4(1983)353

210.

Proposer: Sydney Bulman-Fleming & Edward T. H. Wang 13.1(1982)65

Topic: Find the maximum cardinality of a set of  $n \ge 3$  integers such that  $n_i + n_i > n_k$ 

Solution: Subsets of  $\{1,2,...,n\}$  satisfying i+j>k 14.3(1983)262

211.

Proposer: Edward T. H. Wang 13.2(1982)147

Topic: If  $n \ge 4$  and  $2 \le k \le n-2$ , C(n,k) is never prime. Is it a prime power?

Solution: The number of prime divisors of C(n,k) 14.3(1983)264

212.

Proposer: Michael W. Ecker 13.2(1982)147

Topic: Product of  $1 - x^k$  where w is any nth root of unity

Solution: Generalization of  $(\sin \pi/5)(\sin 2\pi/5) = \sqrt{5}/4$  14.3(1983)265

213.

Proposer: Chico Problem Group 13.2(1982)147

Topic: Questions about limits involving a function and its continuous 1st and 2<sup>nd</sup> derivative

Solution: Lim (as  $x \to \infty$ ) f(x) = 0 versus  $\lim_{x \to \infty} (as x \to \infty) f'(x) = 0$  14.4(1983)356

214.

Proposer: Charles W. Trigg 13.2(1982)148

Topic: Magic square problem

Solution: Magic four squares squares 14.4(1983)356

215.

Proposer: V. N. Murty 13.2(1982)148

Topic: Closed form for the sum of products of ratios of factorials Solution: Vandermonde identity with repetitions 14.5(1983)439

216.

Proposer: Milton P. Eisner 13.3(1982)206

Topic: Expected value involving matching pairs of socks

Solution: \*\*\*\*\*

Proposer: Norman Schaumberger 13.3(1982)206

Topic: Inequalities involving square roots and products of rational fractions

Solution: Bounds for  $\Gamma(x)$   $\Gamma(x + \frac{1}{2})$  14.5(1983)441

218.

Proposer: V. N. Murty 13.3(1982)207

Topic: Sum of a tangent and sine function

Solution: Does  $\tan(3\pi/11 + 4\sin(2\pi/11)) = \sqrt{11}$ ? 14.4(1983)358

219.

Proposer: A. C. Segal 13.3(1982)207

Topic: Sequence of products of cosines approximating  $\pi$  and its error bound

Solution: Vieta's infinite product for  $\pi$  15.1(1984)69

220.

Proposer: Milton P. Eisner 13.3(1982)207

Topic: Choice of 2 payment plans for receiving d dollars

Solution: Plan A or plan B 15.1(1984)70

221.

Proposer: Simeon M. Berman 13.3(1982)207

Topic: Inequality involving the elements of a positive definite matrix

Solution: An inequality for positive definite forms 15.1(1984)71

222.

Proposer: Stanley Rabinowitz 13.3(1982)207

Topic: Probability involving the roll of 4 n-sided dice

Solution: \*\*\*\*\*

223.

Proposer: Warren Page 13.3(1982)207

Topic: Location of the roots of an equation involving the sum of linear reciprocals

Solution: Logarithmic derivative of a polynomial 15.1(1984)72

224.

Proposer: V. N. Murty 13.4(1982)276

Topic: Inequality involving the mean and standard deviation of a set of numbers

Solution: Set mean minus subset mean 15.1(1984)73

225.

Proposer: Norman Schaumberger 13.4(1982)277

Topic: Equation and 3 inequalities involving the functions of angles of a triangle

Solution: Inequalities for a triangle 15.2(1984)164

226.

Proposer: Walter Bluger 13.4(1982)277

Topic: Maximum number of  $1 \times 2 \times 4$  bricks in cube with sides of length 7

Solution: \*\*\*\*\*

227.

Proposer: K. R. S. Sastry 13.4(1982)277

Topic: Necessary & sufficient conditions concerning the sides of a convex quadrilateral

Solution: Orthodiagonal quadrilaterals 15.2(1984)165

Proposer: Gary F. Birkenmeier 13.4(1982)277

Topic: Finding integral Solutions of an algebraic equation

Solution:  $(Z^x - 1)(Z^y - 1) = Z^w + 1$  15.2(1984)166

229.

Proposer: Boon-Yian Ng 13.4(1982)277

Topic: Inequality involving products ratios of integal expressions Solution: Is  $C(n,r)/n^r$  less than  $C(n+1,r)/(n+1)^r$ ? 15.2(1984)168

230.

Proposer: Sydney Bulman-Fleming & Edward T. H. Wang 13.4(1982)277

Topic: Question concerning the mean of a set of average values of a set of numbers

Solution: Mean values of subsets of a finite set 15.3(1984)269

231.

Proposer: Jan List Boal & Jean H. Bevis 13.5(1982)333

Topic: In any number base there is only one palindrome with an even number of digits

Solution: Palindromic primes 15.3(1984)270

232.

Proposer: K. R. S. Sastry 13.5(1982)333

Topic: Forming a larger triangle from 5 existing perfect triangles Solution: Two triangles: each divided perfectly 15.3(1984)271

233.

Proposer: M. Selby 13.5(1982)334

Topic: Inequality involving the sides of a triangle

Solution: Inequality for the sides of a triangle 15.3(1984)272

234.

Proposer: Bertram Kabak 13.5(1982)334

Topic: Equation involving the areas of triangles formed from sides of a parallelogram

Solution: Areas of oriented triangles on a directed line segment 15.4(1984)348

235.

Proposer: Norman Schaumberger 13.5(1982)334

Topic: Inequality involving 4 real numbers and their sum Solution: Generalization of  $a/b + b/a \ge 2$  15.4(1984)349

236.

Proposer: V. N. Murty 13.5(1982)334

Topic: Evaluation an improper logarithmic integral

Solution: Evaluation of  $\{\text{from } 0 \text{ to } \infty\} \ln ((1+x)/(1-x))^2 dx = 15.4(1984)351$ 

237.

Proposer: Thomas E. Elsner 13.5(1982)334

Topic: 4 color problem involving pennies in a plane

Solution: \*\*\*\*\*

238.

Proposer: V. N. Murty 14.1(1983)64

Topic: Inequality involving the sides of a right triangle Solution: Scalene triangle inequality 15.4(1984)352

Proposer: Norman Schaumberger 14.1(1983)64

Topic: The product of 4 distinct non-zero integers can or cannot be a 4<sup>th</sup> power

Solution: Thanks again, Euler 15.5(1984)446

240.

Proposer: K. R. S. Sastry 14.1(1983)64

Topic: Circumcircles, escribed circles and tangents to a triangle

Solution: Circles and centers of triangles 15.5(1984)446

241.

Proposer: Claire Krukenberg & Lawrence Ringenberg 14.1(1983)65

Topic: Finding a closed form for the sum of a series of reciprocal products Solution: On  $\Sigma$  {from m = n to  $\infty$ } (m(m + 1)  $\cdots$  (m + p))<sup>-1</sup> 15.5(1984)448 242.

242.

Proposer: Arnold Lapidus 14.1(1983)65

Topic: Evaluate a determinant using only its trace and traces of its powers

Solution: Newton's formulae 15.5(1984)450

243.

Proposer: Robert E. Shafer 14.2(1983)173

Topic: Proving that the numerator of a sum of fractions is divisible by  $2^{2n}$  Solution: Divisibility property of  $\Sigma$  {from 1 to  $2^n$ } 1/(2k - 1) 16.1(1985)80

244.

Proposer: Michael Filaseta 14.2(1983)173

Topic: Identity for a finite sum of the squares of products of cosecants and cotangents

Solution: Cotangent series 16.1(1985)78

245.

Proposer: Norman Schaumberger 14.2(1983)173

Topic: For which powers does a sum of ratios of odd products to even products converge? Solution: Elementary proof that  $\Sigma ((1\cdot 3\cdot 5\cdots (2n-1))/(2\cdot 4\cdot 6\cdots 2n))^2$  diverges 16.1(1985)78 246.

Proposer: Jerry M. Metzger 14.2(1983)173

Topic: Sequences with arithmetic mean equaling the geometric mean of the 1<sup>st</sup> and last term

Solution: Sequences with  $a_1 + a_2 + ... + a_k = k \sqrt{a_1 a_k}$  16.1(1985)80

247.

Proposer: Mangho Ahuja 14.2(1983)173

Topic: Largest integer not a sum of nonnegative multiples of 2 primes in terms of the primes

Solution: Representation of integers by linear forms 16.2(1985)154

248.

Proposer: M. S. Klamkin 14.2(1983)173

Topic: Terms of ratios and sums of 2 sequences of arithmetic and geometric progressions

Solution: Ratios and sums of progressions 16.2(1985)155

Proposer: K. R. S. Sastry 14.3(1983)260

Topic: Necessary & sufficient condition for a given geometric mean to exist inside a triangle

Solution: Triangles ABC with AB + AC  $\leq \sqrt{2}$  BC 16.2(1985)157

250.

Proposer: Jerry M. Metzger 14.3(1983)260 Topic: For what k is 10<sup>k</sup> - 1 a perfect cube? Solution: When Is 10<sup>k</sup> - 1 a cube? 16.2(1985)159

251.

Proposer: Norman Schaumberger 14.3(1983)260

Topic: Inequality for functions of the 3 sides of a triangle Solution: Consolidation of triangle inequalities 16.2(1985)159

252.

Proposer: Michael W. Ecker 14.3(1983)260

Topic: Find a set of integers so that the sum of any subset does not equal a given integer

Solution: On binary representation of integers 16.2(1985)160

253.

Proposer: M. S. Klamkin 14.3(1983)261

Topic: N &S inequality on the cotangents of angles of a triangle that make it equilateral

Solution: The inequality  $3\Sigma \cot A \ge \Sigma \cot (A/2)$  16.3(1985)224

254.

Proposer: R. S. Luthar 14.3(1983)261

Topic: Finding a function satisfying 3 conditions for x > 0Solution:  $\sqrt{x} (dy/dx) - (y/2\sqrt{x}) = \log x \quad 16.3(1985)226$ 

255.

Proposer: F. Lee Cook 14.4(1983)352

Topic: Algebraic inequality

Solution: Comparison of  $\Sigma$  {from 1 to n}  $k^r$  and  $\int$  {from 1 to n+1}  $x^r dx$  16.3(1985)227

256.

Proposer: Armel Mercer 14.4(1983)352

Topic: A polynomial function, a Maclaurin series and Stirling numbers of the 2<sup>nd</sup> kind

Solution: \*\*\*\*\*

257.

Proposer: Gengzhe Chang 14.4(1983)353

Topic: Necessary & sufficient condition for an inequality on 6 real number to be valid

Solution: Homogeneous inequality 16.3(1985)228

258.

Proposer: Leslie V. Glickman 14.4(1983)353 Topic: Binomial coefficient ratio identity Solution: Combinatorial identity 16.3(1985)229

Proposer: Sanjukta Hota & Kathy Williams 14.4(1983)353

Topic: Inequalities involving roots and products of rational expressions

Solution: Estimation of a product 16.3(1985)230

260.

Proposer: Suresh Ailawadi 14.5(1983)439 Topic: Evaluating a trigonometric integral

Solution: Symmetry method for definite integrals 16.4(1985)305

261.

Proposer: M. S. Klamkin 14.5(1983)439

Topic: Explaining the numerical approximations of the tangent of 89.99...

Solution: Tangent of  $(90 - \varepsilon)^0$  16.4(1985)306

262.

Proposer: Kenneth Fogarty 14.5(1983)439

Topic: Plane separating a tetrahedron into 2 solids of equal volume Solution: Planes through a median of a tetrahedron 16.4(1985)307

263.

Proposer: Charles W. Trigg 14.5(1983)439

Topic: Finding figurate numbers which are the sum of three 3-digit primes

Solution: Prime sums for K-gons 16.4(1985)308

264.

Proposer: R. S. Luthar 14.5(1983)439

Topic: Inequality involving the area and perimeter of a triangle Solution: Isoperimetric inequality for triangles 16.4(1985)309

265.

Proposer: M. S. Klamkin 15.1(1984)68

Topic: Extreme values of the sum of sines of the angles of a triangle

Solution: Triangle inequalities 16.4(1985)310

266.

Proposer: Sydney Bulman-Fleming & Edward T. H. Wang 15.1(1984)68

Topic: Finding the number of intersections of an exponential and a polynomial graph

Solution: Numbers which equal their logarithms 16.4(1985)311

267.

Proposer: Robert E. Shafer 15.1(1984)68

Topic: Inequality involving sums of reciprocals of cubed binomials

Solution: Generalizations of  $\zeta(3) > \frac{1}{4} (\zeta(2))^3$  16.5(1985)417

268.

Proposer: Norman Schaumberger 15.1(1984)69

Topic: Trig identity involving sums of products of secants

Solution: Formula for the difference of two tangents 16.5(1985)419

269.

Proposer: Chico Problem Group 15.1(1984)69

Topic: Find an asymptotic formula for a sum of ratios of binomial coefficients

Solution: Asymptotic formula for the Nth difference of 1/x 16.5(1985)419

Proposer: Martin LaBar 15.1(1984)69

Topic: Can a 3×3 magic square be formed from 9 distinct integral squares?

Solution: \*\*\*\*\*

271.

Proposer: Robert E. Shafer 15.2(1984)163

Topic: Finding the maximum quantity in a certain set

Solution: Permutation of  $x^{(y)}$  16.5(1985)421

272.

Proposer: F. David Hammer 15.2(1984)163

Topic: Partitioning the integers into disjoint sets with range a Fibonacci sequence

Solution: Fibonacci notation for natural numbers 16.5(1985)422

273.

Proposer: R. Shantaram 15.2(1984)164

Topic: Equation involving the areas of faces of a tetrahedron

Solution: Cosine law for tetrahedra 17.1(1986)93

274.

Proposer: Edwart T. H. Wang 15.2(1984)164

Topic: Determining 2 matrices whose squares are zero but whose products are not

Solution: Commuting nilpotent matrices 17.1(1986)96

275.

Proposer: Norman Schaumberger 15.2(1984)164

Topic: Finding the limit of the nth root of a product of integers congruent to 1 mod 3 over n

Solution:  $\lim_{n \to \infty} 1/n \left[ (\alpha + \beta)(2\alpha + \beta) \cdots (n\alpha + \beta) \right]^{1/n} \text{ as } n \to \infty \quad 17.1(1986)97$ 

276.

Proposer: Norman Schaumberger 15.3(1984)266; Corrected: 16.3(1985)223

Topic: Finding zeroes of a polynomial having only positive integral zeroes and satisfying

summation conditions on its coefficients

Solution: The polynomial is  $(x - 2)^{2n}$  17.5(1986)443

277.

Proposer: Fr. Gabe Costa 15.3(1984)267

Topic: Evaluate the sum of squared reciprocals of square free positive integers

Solution: Subseries of  $\Sigma$  n<sup>-2</sup> 17.1(1986)98

278.

Proposer: M. S. Klamkin 15.3(1984)267

Topic: Determine (A - I)<sup>-1</sup> for a matrix, A, satisfying a cubic matrix equation

Solution: Inverse of the matrix A - I 17.2(1986)185

279.

Proposer: K. R. S. Sastry 15.3(1984)267

Topic: Necessary & sufficient condition that a concyclic trapezoid is isosceles

Solution: Trapezoids which have inscribed circles 17.2(1986)187

Proposer: J. Howard S. Kane & C. Searcy 15.3(1984)267

Topic: Prove that e is the limit of a ratio of consecutive terms of a given sequence

Solution: Rate of divergence of  $\Sigma$  1/n 17.2(1986)188

281.

Proposer: Charles W. Trigg 15.4(1984)346

Topic: Palindromic triangular numbers in base 9

Solution: Palindromic triangular numbers in base nine 17.2(1986)188

282.

Proposer: M. S. Klamkin 15.4(1984)346 Topic: Altering a familiar trig identity

Solution: Functional equation  $(f(x) \cdot f(y))/(g(x) \cdot g(y)) = (f(x) - f(y))/(g(x) - g(y))$  17.3(1986)250

283.

Proposer: Terry Shell 15.4(1984)347

Topic: Finding the number of dice necessary to maximize the probability of getting n 6's

Solution: How many dice minimize this probability? 17.3(1986)251

284.

Proposer: Gary Walls 15.4(1984)347

Topic: Finding values that guarantee convergence of an improper integral

Solution: Sums of partial integrals 17.3(1986)251

285.

Proposer: K. R. S. Sastry 15.4(1984)347

Topic: Necessary & sufficient condition concerning a triangle's excircle and inscribed circle

Solution: Incircle and excircle revisited 17.3(1986)252

286.

Proposer: Bertram Kabak 15.5(1984)445

Topic: Necessary & sufficient condition for a triangle to be equilateral

Solution: Equilateral triangle trigonometry 17.3(1986)253

287.

Proposer: Harry Sedinger 15.5(1984)445

Topic: Convergence of a sequence from a function of the integer and fractional part of x>1

Solution: Sequence with algebraic limit 17.3(1986)254

288.

Proposer: R. S. Luthar 15.5(1984)445

Topic: Trigonometric - exponential integral Solution:  $\int (\tan^2 x - \tan x)e^{-x} dx$  17.4(1986)361

289.

Proposer: Norman Schamberger 15.5(1984)446

Topic: Trigonometric sine inequality

Solution: Comparability of  $\sin(\sqrt{xy})$  and  $\sqrt{(\sin x \cdot \sin y)}$  17.4(1986)362

290.

Proposer: Gengzhe Chang 15.5(1984)446

Topic: Limit of a sequence defined by an integral multiplied by a binomial coefficient

Solution: Limit of a sum of binomial probabilities 17.4(1986)364

Proposer: Heinz-Jürgen Seiffert 16.1(1985)74

Topic: Integral inequality

Solution: Inequality for convex functions 17.5(1986)444

292.

Proposer: Peter Sisler 16.1(1985)74
Topic: Algebraic summation identity

Solution: Series for log x on the interval  $0 < x \le 2$  17.5(1986)446

293.

Proposer: Norman Schaumberger 16.1(1985)75
Topic: Comparing ratios of sums of trig functions

Solution: Inequality for trigonometric series 17.5(1986)447

294.

Proposer: Russell Euler 16.1(1985)75 Topic: Polar coordinate product identity

Solution: Factorization of  $|z^p - 1|^2$  17.5(1986)448

295.

Proposer: Verne R. Sanford 16.1(1985)75

Topic: Necessary & sufficient condition that (f/g)' = f'/g' holds in some interval

Solution: When does (h/g)' = h'/g'? 18.1(1987)70

296.

Proposer: Edilio Escalone F. 16.2(1985)153

Topic: Finding functions that satisfy a mean value type equation Solution: Solution of f(x) - g(y) = (x - xy)h(x + y) 18.4(1987)341

297.

Proposer: M. S. Klamkin 16.2(1985)153

Topic: Show that a function of homogeneous functions is also homogeneous

Solution: Functionally dependent homogeneous functions 18.1(1987)72

298.

Proposer: Roger B. Nelson 16.2(1985)153

Topic: Equivalence and congruence classes of triangles in a regular n-gon Solution: Number of triangles equals number of partitions 18.1(1987)72 299.

Proposer: Arnold Lapidus 16.2(1985)154

Topic: Optimal strategy sought in a coin tossing game

Solution: Game of the first occurring head-tail sequence 18.1(1987)74

300.

Proposer: K. R. S. Sastry 16.2(1985)154

Topic: Necessary & sufficient condition involving a triangle's sides and an angle bisector

Solution: Triangles with a double angle 18.1(1987)76

301.

Proposer: Stephen Plett 16.3(1985)223

Topic: Number of nonsymmetrical ways to label a cube

Solution: Counting colorful cubes 18.2(1987)161

Proposer: Gao Ling 16.3(1985)223

Topic: Necessary & sufficient condition for an inequality involving areas and

semi-perimeters of 2 triangles

Solution: Inequality for parts of two triangles 18.2(1987)163

303.

Proposer: Weixuan Li & Edward T. H. Wang 16.3(1985)224

Topic: Algebraic inequality involving 4 real numbers

Solution: Inequalities for rearrangements of powers 18.2(1987)164

304.

Proposer: Hüseyin Demir 16.3(1985)224

Topic: Necessary & sufficient condition for a circle to be inscribed in a convex quadrilateral

Solution: Inscriptable quadrilaterals 18.2(1987)165

305.

Proposer: Norman Schaumberger 16.3(1985)224

Topic: Finding real numbers that satisfy a given algebraic inequality

Solution: Pigeon holes for ten cubes 18.2(1987)166

306.

Proposer: Sudhir Kumer Goel 16.4(1985)304

Topic: Evaluating the limit of a product of roots of an even powered binomial

Solution: Definite integral 18.3(1987)249

307.

Proposer: Chico Problem Group 16.4(1985)304

Topic: Finding the limit of a function of the number of digits in  $n_k$ !

Solution: When does n! Have n digits? 18.3(1987)250

308.

Proposer: M. S. Klamkin 16.4(1985)304

Topic: Evaluate all 3<sup>rd</sup> order derivatives of 3<sup>rd</sup> powers of a trig expression

Solution: Faà di Bruno's formula is applied 18.3(1987)250

309.

Proposer: Clark Kimberling 16.4(1985)306

Topic: Do all triangles have a tangency point?

Solution: Tangency points of a triangle 18.3(1987)251

310.

Proposer: Robert E. Shafer 16.4(1985)306

Topic: Bounding the error in estimating the sum of a function converging to  $\pi$ 

Solution: Slow road to pi 18.3(1987)252

311.

Proposer: Mike Chamberlain 16.5(1985)416

Topic: Finding values for which a sequence of trigo integrals converge

Solution: Limit  $q^p \beta(p,q) = \Gamma(p)$  as  $q \to \infty$  18.4(1987)343

Proposer: Francisco J. Navarro-Bermudez 16.5(1985)416

Topic: Characterize differentiable functions satisfying a kind of mean value theorem

Solution: Mean value theorem for polynomials 18.4(1987)344

313.

Proposer: M. S. Klamkin 16.5(1985)416

Topic: Is the origin a minimum point of a surface tangent to the x-y plane?

Solution: Normal selections at a saddle point 18.5(1987)426

314.

Proposer: Peter A. Lindstrom 16.5(1985)417

Topic: Find all differentiable functions satisfying a chain-type product rule

Solution: \*\*\*\*\*

315.

Proposer: Dale Meinhold 16.5(1985)417

Topic: Finding the expected value for the number of die tosses to obtain all 6 faces

Solution: Hexahedral waiting time 18.5(1987)427

316.

Proposer: M. S. Klamkin 17.1(1986)92

Topic: Summation inequality involving 5 given positive quantities

Solution: {Cyclic}  $\Sigma$  (  $a_1 a_2 a_3 / a_4 a_5$ )<sup>4</sup>  $\geq$  {cyclic}  $\Sigma a_1 a_2^2 a_3 18.1(1987)428$ 

317.

Proposer: Huseyin Demir 17.1(1986)92

Topic: Independence of areas of a parallelogram, a star pentagon and another pentagon

Solution: Star polygons inscribed in a parallelogram 18.5(1987)428

318.

Proposer: Harvey J. Fletcher 17.1(1986)92

Topic: Finding initial values of a sequence to guarantee convergence

Solution: Convergence of  $X_{n+1} = b - c/X_n = 18.5(1987)429$ 

319,

Proposer: Richard J. Johnsonbaugh 17.1(1986)93

Topic: Show that 2 given sequence are monotonic and find their limits Solution: Monotonicity of  $(x^{x+1}/(x+1)^x)^x/\Gamma(x+1)$  18.5(1987)431 320.

Proposer: Norman Schaumberger 17.1(1986)93

Topic: Inequality involving rations of natural number expressions

Solution: Bounds for  $\{n/(n+1)\}^{1/(n+1)}$  19.1(1988)82

321.

Proposer: M. S. Klamkin 17.2(1986)184

Topic: Prove that an algebraic ratio is between 1 and 2

Solution: Bounds for  $\{(x - \frac{1}{2})^{x - \frac{1}{2}}(x + \frac{1}{2})^{x + \frac{1}{2}}\}/x^{2x}$  19.1(1988)84

322.

Proposer: Anon 17.2(1986)184

Topic: Finding a generalization of a function from a Pascal program Solution: Simplifying a function defined in Pascal 19.1(1988)86

Proposer: Eugene Levine 17.2(1986)185

Topic: Solving a 20<sup>th</sup> degree polynomial equation

Solution:  $(x^2 - 9x - 1)^{10} + 99x^{10} = 10x^9 (x^2 - 1)$  19.1(1988)87

324.

Proposer: Florentine Smarandache 17.2(1986)185

Topic: Find all integers whose fixed multiple of Euler's  $\varphi$ -function divide the integer

Solution: When is  $n/\varphi(n)$  an integer  $\le 3? > 3?$  19.2(1988)187

325.

Proposer: Larry Hoehn 17.2(1986)185

Topic: Finding the arithmetic mean of 2 sides of a convex quadrilateral

Solution: Cyclic quadrilaterals and broken chords 19.2(1988)188

326.

Proposer: David Sack 17.3(1986)249

Topic: Largest subset serving as the domain for a function defined by an infinite series

Solution: Domain of convergence of  $\Sigma$  {from n=2 to  $\infty$ } n<sup>-p</sup> (log n)<sup>-q</sup> 19.2(1988)189

327.

Proposer: Warren B. Ordon 17.3(1986)249

Topic: Find the limit of the reciprocal of a triangular number times a given sum

Solution: Limit of Riemann sums 19.2(1988)190

328.

Proposer: F. Smarandache 17.3(1986)249

Topic: Necessary & sufficient condition that p and p + 2 are prime

Solution: Prime pairs and Wilson's theorem 19.2(1988)191

329.

Proposer: Edward T. Wang 17.3(1986)250

Topic: Finding the limit of a sequence defined on the median of 2 rational numbers

Solution: Limit of mediants 19.2(1988)192

330.

Proposer: M. S. Klamkin 17.3(1986)250

Topic: Extreme value of a sum of 3 fractions in 3 variables Solution: Extreme values of  $\sum x^2/(x + yx)$  19.3(1988)291

331.

Proposer: Robert E. Shafer 17.4(1986)360

Topic: Inequalities for the area, semi-perimeter and tangents of the angles in a triangle

Solution: Inequalities for sides of a triangle 19.3(1988)292

332.

Proposer: M. S. Klamkin 17.4(1986)360

Topic: Maximum value of the circumradius of a circle with an inscribed quadrilateral

Solution: Maximum circumradius of a variable triangle 19.3(1988)294

333.

Proposer: Vis Upatrisringa 17.4(1986)361 Topic: Complex number identity for  $\sin^2 \theta$ 

Solution: Hyperbola in the complex plane squared 19.4(1988)371

Proposer: Clark Kimberling 17.4(1986)361

Topic: Find a Euclidean construction for the limit of a point sequence defined in a triangle

Solution: Contracting infinite sequence of triangles 19.4(1988)372

335.

Proposer: Arthur C. Segal 17.4(1986)361

Topic: Finding a closed form for an infinite alternating sum of a ratio of polynomials

Solution: Series of values of a rational function 20.1(1989)69

336.

Proposer: Robert E. Shafer 17.5(1986)442

Topic: Inequalities involving a function defined for reciprocals of positive numbers

Solution: Inequality proved by the Laplace transform 19.5(1988)449

337.

Proposer: M. S. Klamkin 17.5(1986)442

Topic: Inequality involving sums of fractions of 4 positive numbers Solution: If  $\prod a = 1$ , then  $\sum a^3 \ge Max \{\sum a, \sum 1/a\}$  19.5(1988)450

338.

Proposer: Norman Schaumberger 17.5(1986)443

Topic: Limit of ratios of sums from subsequences of the harmonic sequence

Solution: The probability of a number being square free 19.4(1988)373

339.

Proposer: Geoffrey A. Kandall 17.5(1986)443

Topic: Equality involving ratios of distance from the sides of a triangle and 3 interior points

Solution: Ratio of ratios for three concurrent lines 20.1(1989)75

340.

Proposer: James Foster 17.5(1986)443

Topic: Probability for consecutive heads in a coin toss experiment

Solution: Heads before tails 20.1(1989)75

341.

Proposer: Martin Gardner 18.1(1987)69

Topic: Determining a criterion for a starting pattern for winning a peg removable puzzle

Solution: Jumping pegs 20.1(1989)78

342.

Proposer: Otto Bintz 18.1(1987)69

Topic: Finding the average squareness of all natural numbers Solution: Average squareness of natural numbers 20.2(1989)164

343.

Proposer: M. S. Klamkin 18.1(1987)69 Topic: Algebraic division problem

Solution: Polynomial division 20.2(1989)166

344.

Proposer: Craig Bailey & Bruce Richter 18.1(1987)70 Topic: Finding positions of sets in lexicographic order

Solution: Lexicographic ordering of k-subsets of an n-set 20.2(1989)167

Proposer: Sydney Balman-Fleming 18.1(1987)70

Topic: Find long sequences of natural numbers, none of which is a sum of 2 squares Solution: Sequences of integers not representable as a sum of two squares 20.2(1989)168

346.

Proposer: Peter Andrews & Edward T. H. Wang 18.2(1987)160

Topic: What point in or on a triangle maximizes the sum of distances from it vertices?

Solution: Opposite of the Fermat point 20.2(1989)169

347.

Proposer: Larry Hoehn 18.2(1987)160

Topic: Product of ratios involving mutually trisecting cevians in a triangle

Solution: Generalization of Ceva's theorem 20.2(1989)170

348.

Proposer: Norman Schaumberger 18.2(1987)160

Topic: Inequalities involving powers of 3 and a ratio of factorials

Solution: Comparison of the probabilities  $[(kn)!/(n!)^k]k^{-nk}$  20.2(1989)171

349.

Proposer: John W. Lindsay & William Watkins 18.2(1987)161 Topic: Uniqueness of representation of integers in number base -2

Solution: Negative bases 20.3(1989)257

350.

Proposer: Florentine Smarandache 18.2(1987)161

Topic: Solve a system of 2 equations in 3 variables

Solution: Two Diophantine equations 20.3(1989)258

351.

Proposer: R. S. Luthar 18.3(1987)248

Topic: Inequality involving the sides of a right triangle

Solution: Right triangle inequality 20.3(1989)259

352.

Proposer: Dave Ohlsen 18.3(1987)248

Topic: Equality involving permutations and the greatest integer function

Solution:  $\Sigma P_k^n = [n!e] 20.3(1989)260$ 

353.

Proposer: Clark Kimberling 18.3(1987)248

Topic: Proof that a triangle has an interior point on 3 congruent circles tangent to its sides

Solution: Congruent bitangent circles in a triangle 20.3(1989)261

354.

Proposer: Alvin Tirman 18.3(1987)248

Topic: Is a certain triangle inside an integral right triangle also integral?

Solution: Nested integer-sided right triangles 20.3(1989)262

355.

Proposer: Robert E. Shafer 18.3(1987)249

Topic: Divisibility of the sum of powers of odd integers by even and odd powers of 2

Solution: Factors of 2 in  $\Sigma$  {from k=1 to 2<sup>n</sup>} (2k - 1)<sup>s</sup> 20.3(1989)263

Proposer: Sydney Bulman-Fleming 18.4(1987)340

Topic: Inequalities involving the sequence of prime numbers Solution: Application of Bertrand's postulate 20.3(1989)265

357.

Proposer: Chico Problem Group 18.4(1987)341

Topic: The Euler-Mascheroni constant and functions satisfying equality of integrals

Solution: Construction of a class of continuous functions 21.4(1990)335

358.

Proposer: Florentine Smarandache 18.4(1987)341

Topic: Find values of n which make a function involving n and the  $\sqrt{2}$  integral

Solution: Perfect squares in a sequence 21.4(1990)336

359.

Proposer: Gregg Patruno 18.4(1987)341

Topic: Inequality involving factorials and products of powers of integers Solution: A.G.M. Inequality applied to binomial coefficients 20.4(1989)344

360.

Proposer: J. H. Webb 18.4(1987)341

Topic: Inequalities involving natural numbers and their square roots as exponents

Solution:  $n^{\sqrt{(n+1)}}$  versus  $(n+1)^{\sqrt{n}}$  20.4(1989)345

361.

Proposer: Mohammad K. Azarian 18.5(1987)425

Topic: Inequality involving sums of sines and cosines of reciprocals of natural numbers

Solution: Telescoping series 20.4(1989)346

362.

Proposer: Bruce Deardon 18.5(1987)425

Topic: Diophantine equation in 2 variables with integral coefficients Solution: Quadratic Diophantine equations in two letters 20.4(1989)346

363.

Proposer: Thomas P. Dence 18.5(1987)425

Topic: Maximum cardinality of the set of equal values for 2 different real-valued functions

Solution: An uncountable number of intersections 21.1(1990)66

364.

Proposer: Thomas M. Green 18.5(1987)426

Topic: Locus of a point having exactly 2 normals to a parabola

Solution: Evolute of a parabola 20.4(1989)348

365.

Proposer: Mary Spruill Kilgore 18.5(1987)425

Topic: The incenters of triangles formed from vertices of a cyclic quadrilateral form a

rectangle

Solution: Incentral rectangle of a cyclic quadrilateral 20.4(1989)349

Proposer: Ambati Jeya Krishna 19.1(1988)81

Topic: Inequalities involving sides inradius and circumradius of a triangle

Solution: Reappearance of a triangle triple inequality 20.4(1989)352

367

Proposer: Robert E. Shafer 19.1(1988)81

Topic: Evaluating the alternating sum of binomial coefficients Solution: Chebyshev polynomials of the second kind 20.4(1989)353

368.

Proposer: M. S. Klamkin 19.1(1988)81

Topic: Generalize a 2-variable complex number identity to 3 variables Solution: Parallelopiped law for complex numbers 20.5(1989)443

369.

Proposer: Martin Feuerman 19.1(1988)82

Topic: Finding an invertible 2×2 matrix from a non-invertible one with no saddle point

Solution: Saddle point condition for invertibility 20.5(1989)445

370.

Proposer: Norman Schaumberger 19.1(1988)82

Topic: Product inequality involving the powers of 3 positive numbers Solution: Application of the extended Chebyshev inequality 20.5(1989)445

371.

Proposer: Zun Shan & Edward T. H. Wang 19.2(1988)186 Topic: Solving a 2-variable system of 2 cubic equations Solution: Nonlinear system with symmetry 20.5(1989)447

372.

Proposer: Eugene Levine 19.2(1988)186

Topic: Inequality involving n points on a unit circle

Solution: Mean length of all chords through a point of a circle 20.5(1989)448

373.

Proposer: Robert E. Shafer 19.2(1988)186

Topic: Finding 9 points on a sphere with 4 equidistant nearest neighbors

Solution: Nine points on a sphere 21.1(1990)66

374.

Proposer: Murray S. Klamkin 19.2(1988)186

Topic: Necessary & sufficient condition involving an in-&-circumcircle and sides of a

quadrilateral

Solution: Quadrilaterals having incircles and perpendicular diagonals 20.5(1989)448

375.

Proposer: Norman Schaumberger 19.2(1988)187

Topic: Summation-product inequality for a sequence of 4 positive numbers

Solution:  $\sum a_i^{27} / \prod a_i \ 21.1(1990)68$ 

Proposer: R. S. Luthar 19.3(1988)290

Topic: Equality of sums involving points on the sides of a triangle

Solution: Reciprocals of triangle sides 20.5(1989)449

377.

Proposer: M. S. Klamkin 19.3(1988)290

Topic: Finding the maximum value of an 8<sup>th</sup> degree polynomial

Solution: Chebyshev polynomial 20.5(1989)450

378.

Proposer: Edward T. H. Wang 19.3(1988)291

Topic: Evaluate the determinant with entries being multi-selection numbers

Solution: The determinant of a multi-selection matrix 21.3(1990)247

379.

Proposer: Mohammad K. Azarian 19.3(1988)291 Topic: Trigonometric summation inequality

Solution: A trigonometric inequality 21.3(1990)248

380.

Proposer: Stephen Plett 19.3(1988)291

Topic: Partitioning natural numbers into 3 numbers representing the sides of a triangle

Solution: Triangular partitions 21.4(1990)337

381.

Proposer: Mohammad K. Azarian 19.4(1988)370

Topic: Least upper bound on the limit involving the square root of a double sum

Solution: A bounded double sum 21.1(1990)69

382.

Proposer: Parviz Khajeh-Khalili 19.4(1988)370

Topic: Summation inequality for the cosines of angles of an inscribed quadrilateral

Solution: A trigonometric inequality for quadrilaterals 21.1(1990)69

383.

Proposer: Murray S. Klamkin 19.4(1988)370

Topic: Proving a statement about the difficulty establishing a triangle inequality

Solution: A not-so-difficult triangle inequality 21.1(1990)70

384.

Proposer: Thomas P. Dence 19.4(1988)371

Topic: Algebraic inequality

Solution:  $2 \le x \le y$  implies  $y^{x+1} \le xy^y = 21.1(1990)701$ 

385.

Proposer: Kazem . Sedati 19.4(1988)371

Topic: Establishing the value of a product of cosines

Solution:  $\cos(\pi/14)\cos(3\pi/14)\cos(5\pi/14) = \sqrt{7/8} + 21.1(1990)71$ 

386.

Proposer: Eugene Levine 19.5(1988)448

Topic: Equality involving the sum of large digits in powers of 2

Solution: A sum of large digits 21.2(1990)151

Proposer: Larry Hoehn 19.5(1988)448

Topic: Proving a ratio of powers of sums and differences of natural numbers is integral

Solution: Division by a square 21.2(1990)152

388.

Proposer: Morris Wald 19.5(1988)448

Topic: Probability that 3 positive integers < 1001 are sides of a triangle

Solution: Triangles from random integers 21.2(1990)153389.

Proposer: M. S. Klamkin 19.5(1988)449

Topic: Finding real factors of a quadratic binomial of 3 variables

Solution: Differences of cubes 21.2(1990)154

390.

Proposer: Roger B. Nelsen 19.5(1988)449

Topic: Smallest right triangle having an integral square inscribed on the hypotenuse

Solution: Squares in a Pythagorean triangle

391.

Proposer: Murray S. Klamkin 20.1(1989)68

Topic: Non-linear Diophantine equation in 3 variables Solution: A rational Diophantine equation 21.2(1990)155

392.

Proposer: Robert Jones 20.1(1989)68

Topic: Algebraic- trigonometric inequality

Solution: An inequality for the sine 21.2(1990)156

393.

Proposer: Ginger Bolton 20.1(1989)68

Topic: Possibile summation of products equality Solution: A sum of products 21.2(1990)156

394.

Proposer: John F. Loase 20.1(1989)69

Topic: For a polynomial, f, is f(k) the  $k^{th}$  digit in the decimal expansion of  $\sqrt{2}$ ?

Solution: Polynomial generation of  $\sqrt{2}$  21.3(1990)249

395.

Proposer: Murray S. Klamkin 20.1(1989)69

Topic: Inequality for the areas of a triangle and the one formed by extended altitudes

Solution: An area inequality for two triangles 21.3(1990)249

396.

Proposer: Alan Wayne 20.2(1989)163

Topic: Alphanumeric puzzle

Solution: 46933 = Gauss 21.3(1990)250

397.

Proposer: Eugene Levine 20.2(1989)163

Topic: Determinant of a matrix formed by adding 1 to the elements of another matrix

Solution: The determinant of a sum 21.3(1990)251

398

Proposer: Brian Anderson & Barry Brunson 20.2(1989)163

Topic: Does the sum of distances from equally spaced points on a circle to a diameter

depend on the diameter selected?

Solution: The independence of a circular sum 21.3(1990)252

399.

Proposer: Norman Schaumberger 20.2(1989)164

Topic: Evaluate a sum of arctangents

Solution: An old arctangent series reappears 21.3(1990)253

400.

Proposer: Murray Klamkin 20.2(1989)164

Topic: Equality of simplexes formed from antipodal points on an n-dimensional sphere

Solution: Simplicial volumes 21.4(1990)337

401.

Proposer: Alan Wayne 20.3(1989)256

Topic: Curve traced by highest point of water from a moving hose

Solution: The path of water 21.4(1990)338

402.

Proposer: Norman Schaumberger 20.3(1989)256

Topic: Equality of sums of 5<sup>th</sup> and 7<sup>th</sup> roots of quantities involving square roots of 5

Solution: Sums of roots 21.4(1990)339

403.

Proposer: Howard Reinhardt 20.3(1989)256

Topic: Bounds on the average number of children in families in a certain community

Solution: Average children 21.4(1990)340

404.

Proposer: Murray Klamkin 20.3(1989)256

Topic: Prove a sequence of ratios of powers of natural numbers is increasing

Solution: An increasing sequence 21.4(1990)340

405.

Proposer: Bill Wardlaw 20.3(1989)257

Topic: Necessary & sufficient condition for an inner product inequality of n-dim vectors

Solution: A scalar product inequality 21.5(1990)424

406.

Proposer: Murray Klamkin 20.4(1989)343

Topic: Inequality involving ratios of 3 positive numbers

Solution: A Muirhead inequality 21.5(1990)424

407.

Proposer: Murray Klamkin 20.4(1989)343 Topic: Evaluating an algebraic integral

Solution: Integration by (almost any) substitution 21.5(1990)425

Proposer: Clark Kimberling 20.4(1989)343

Topic: Concurrent lines and the excenters of a triangle Solution: A case of concurrent lines 21.5(1990)426

409.

Proposer: S. A. Banawan 20.4(1989)344

Topic: Evaluate an alternating sum of binomial coefficients over a quadratic

Solution: A binomial identity reappears 21.5(1990)427

410.

Proposer: Harry Sedinger 20.4(1989)344

Topic: Characterizing certain sequences of odd integers

Solution: An old sum 21.5(1990)428

411.

Proposer: Murray Klamkin 20.5(1989)442

Topic: Elementary symmetric functions on what must be a unique set Solution: Power series and symmetric polynomials 21.5(1990)429

412.

Proposer: Edward F. Vitek 20.5(1989)442

Topic: Find the limit of a sequence of ratios of positive numbers and their logarithms

Solution: A bounded monotone sequence converges 21.5(1990)429

413.

Proposer: K. R. S. Sastry 20.5(1989)442

Topic: Two equalities arising from 2 lines and reflected rays

Solution: Similar trapezoids 22.1(1991)71

414

Proposer: Norman Schaumberger 20.5(1989)443

Topic: Squeezing ln 2 between 2 sums Solution: An inequality of ln 2 22.1(1991)71

415.

Proposer: Eugene Levine 20.5(1989)443

Topic: Evaluate the infinite product of the ratio of 2 algebraic quantities

Solution: An infinite product for  $\sqrt{2}$  22.1(1991)72

416.

Proposer: Joanne Harris 21.1(1990)65

Topic: Exponential inequality

Solution: An exponential inequality 22.1(1991)73

417.

Proposer: K. R. S. Sastry 21.1(1990)65

Topic: Questions concerning distances from the incenter and an excenter of a triangle

Solution: Of triangles and trapezoids 22.1(1991)74

418.

Proposer: Norman Schaumberger 21.1(1990)65

Topic: Inequalities on products of integral powers and the exponential function

Solution: Bounds for  $\prod \{\text{from } k = 1 \text{ to } n\} k^k 22.1(1991)74$ 

Proposer: Neville Robbins 21.1(1990)66

Topic: Necessary & sufficient condition that a cosine function is rational

Solution: A rational cosine 22.1(1991)75

420.

Proposer: Edward T. H. Wang 21.1(1990)66

Topic: Inequalities involving binomial coefficients, powers of 2 and the square root of 2

Solution: Bounds for central binomial coefficients 22.1(1991)76

421.

Proposer: Stanley Rabinowitz 21.2(1990)150

Topic: Equality of 2 sides of a triangle depending on its median and 2 inscribed circles

Solution: An isosceles triangle 22.2(1991)168

422.

Proposer: M. Riazi-Kermani 21.2(1990)150

Topic: Probability that the roots of a quadratic equation are real

Solution:  $d^2/d\alpha^2$  Pr {the roots of  $x^2 + ax + b = 0$ , |a|,  $|b| \le \alpha$ , are real} 22.2(1991)168

423.

Proposer: Mohammad K. Azarian 21.2(1990)150

Topic: Improper integral involving logarithms of 2 algebraic functions

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425.

Proposer: David Vaughan & Edward T. H. Wang 21.2(1990)150

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426.

Proposer: Norman Schaumberger 21.3(1990)246

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427.

Proposer: Mohammad K. Azarian 21.3(1990)246

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428.

Proposer: David Doster 21.3(1990)246

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431.

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432.

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433.

Proposer: Nicholas Passell 21.4(1990)334

Topic: Limit of an algebraic function multiplied by an integer satisfying an inequality

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434.

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435.

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437.

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438.

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442.

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443.

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444.

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445.

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452.

Proposer: David G. Hartz 22.3(1991)255

Topic: Sums of k positive integers yield perfect squares for what k?

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453.

Proposer: Zeev Barel 22.3(1991)255

Topic: Find cluster points in an infinite walking pattern Solution: A vacillating mathematician 23.3(1992)250

454.

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455.

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Topic: Necessary & sufficient condition for divisibility in a base N expansion of a proper

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457.

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458.

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Solution:  $x_1^{n+1} + x_2^{n+1} + \dots + x_n^{n+1} \ge x_1 x_2 \dots x_n (x_1 + x_2 + \dots + x_n)$  23.4(1992)344

459.

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460.

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462.

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463.

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Topic: Calculating matrix products given the entries in the product of 3 unknown matrices

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464.

Proposer: Frank Schmidt 22.5(1991)444

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465.

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Topic: Inequality involving a sequence of positive numbers

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466.

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Solution: The area of a lattice quadrilateral 24.1(1993)96

467.

Proposer: Stanley Rabinowitz 23.1(1992)69

Topic: Given the ratios of the cosines of angles in a triangle, find ratios of the sides

Solution: Cos A:  $\cos$  B:  $\cos$  C = 2:9:12  $\Rightarrow$  a:b:c: = 6:5:4 24.1(1993)97

468.

Proposer: Murray Klamkin & Andy Liu 23.1(1992)69

Topic: Inequalities involving logarithms and a sequence of improper integrals

Solution: Bounds on  $\int \{\text{from 1 to } \infty \} dx/(1+x^{n+1}) = 24.1(1993)97$ 

469.

Proposer: K. R. S. Sastry 23.1(1992)70

Topic: Arithmetic progression of length 49 and square sums of squares

Solution: A sum of 49 squares 24.1(1993)99

470.

Proposer: William Wardlaw 23.1(1992)70

Topic: Finding if a trigonometric limit exists

Solution:  $\lim 1/(n \sin n)$  does not exist 24.1(1993)99

471.

Proposer: David Doster 23.2(1992)162

Topic: Lebesgue measure of a set yielding an inequality of bracket functions

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Proposer: Ioan Sadoveanu 23.2(1992)162

Topic: Limits of ratios of members of a decreasing set of real numbers

Solution: Limits of ratios of positive real numbers 24.2(1993)185

473.

Proposer: K. R. S. Sastry 23.2(1992)162

Topic: Necessary & sufficient condition that a triangle is self-median Solution: A characteristic of self-median triangles 24.2(1993)186

474.

Proposer: Zhang Zaiming 23.2(1992)163

Topic: Find the determinant of a given matrix

Solution: A "determinant" for Pascal's triangle 24.2(1993)188

475.

Proposer: Seung-Jin Bang 23.2(1992)163

Topic: Equality of 2 infinite sums of reciprocals of natural numbers

Solution:  $\Sigma (1 + 1/2 + \dots + 1/(n+1)) 1/(n(n+1)) = 2$  from  $\{n = 1 \text{ to } \infty\}$  24.2(1993)189

476.

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477.

Proposer: Norman Schaumberger 23.3(1992)247 Topic: Trig identity involving sines of 3 angles

Solution: Another trigonometric identity 24.3(1993)272

478.

Proposer: K. R. S. Sastry 23.3(1992)247

Topic: Determining a cubic polynomial to guarantee zeroes in arithmetic progression

Solution: Arithmetic progression of roots 24.3(1993)274

479.

Proposer: David Hamilton & Pat Stewart 23.3(1992)247

Topic: Determining if a given matrix is invertible

Solution: A class of nonsingular matrices 24.3(1993)275

480.

Proposer: Ioan Sadoveanu 23.3(1992)248

Topic: Necessary & sufficient condition that certain triangle is equilateral

Solution: Altitudes of an Equilateral Triangle 24.3(1993)275

481.

Proposer: Leonard Gillman 23.4(1992)340

Topic: Find an example satisfying restrictions on lower and upper Riemann sums

Solution:  $L_n > L_{n+1}$  and  $U_n < U_{n+1}$  24.4(1993)378

482.

Proposer: Ioan Sadoveanu 23.4(1992)340

Topic: Prove equality on products of distances from points on the incircle of a triangle

Solution: An incircle invariant 24.4(1993)379

Proposer: Murray Klamkin 23.4(1992)340

Topic: Determine the general term of a sequence of powers given n initial conditions

Solution: Determinant of a power sum 24.4(1993)380

484.

Proposer: S. A. Patil & D. S. Hawkins 23.4(1992)341

Topic: Probability of real roots for a cubic with randomly chosen coefficients in [0,1]

Solution: The probability that the roots of a cubic are real 24.4(1993)382

485.

Proposer: Norman Schaumberger 23.4(1992)341

Topic: Tower power inequalities on 2 positive numbers Solution: An inequality for composite powers 24.4(1993)384

486.

Proposer: Jyotirmoy Sarkar 23.5(1992)435

Topic: Equality of ratios of distances constructed in a triangle

Solution: Constant ratios in a triangle 24.5(1993)475

487.

Proposer: Greg Neumer 23.5(1992)435

Topic: Finding values which permit a limit for a recurring sequence Solution: For what  $x_0$  does  $x_{n+1} = 1/(x_n + 1)$  converge? 24.5(1993)476

488.

Proposer: Murray Klamkin & Andy Liu 23.5(1992)435

Topic: Probability of 2 walkers meeting in a random walk exercise

Solution: A random walk on a square lattice 24.5(1993)477

489.

Proposer: Ioan Sadoveanu 23.5(1992)436

Topic: Determine the convergence and bounds on the limit of a given sequence

Solution:  $e \le \lim u_n \le 1 + e = 24.5(1993)478$ 

490.

Proposer: Jiro Fukuta 23.5(1992)436

Topic: Find the extrema for the area of a quadrilateral inscribed in a circle

Solution: Extremal inscribed quadrilateral 24.5(1993)479

491.

Proposer: Michael Handelsman 24.1(1993)95

Topic: Find a polynomial given the derivative of its ratio with  $x^n$ 

Solution: Polynomial palindromes 25.1(1994)65

492.

Proposer: Norman J. Finizio & James T. Lewis 24.1(1993)95

Topic: Finding the number of balanced arrangements of  $\{1, 2, ..., 2n\}$ 

Solution: Balanced circular arrangements 25.1(1994)66

493.

Proposer: K. R. S. Sastry 24.1(1993)95

Topic: What points guarantee the sum of ratios of distance in a pentagon to be a constant?

Solution: A constant from a pentagon 25.1(1994)66

Proposer: Frank Schmidt 24.1(1993)96

Topic: Find a formula for the number of matrices with a fixed set of eignevalues

Solution: Counting eigenvalues over Z/2Z 25.1(1994)67

495.

Proposer: William R. Klinger 24.1(1993)96

Topic: Critical points harmonically dividing the roots of a cubic polynomial

Solution: An impossible harmonic division 25.1(1994)69

496.

Proposer: Robert J. Blodgett 24.2(1993)183

Topic: Determine positive integers whose digits reverse if added to itself in any base

Solution: Double-reversing numbers 25.2(1994)158

497.

Proposer: Edward Aboufadel 24.2(1993)183

Topic: Quickly solve Arnold's limit problem concerning a ratio of sine and tangents

Solution:  $\lim \{\text{from } x \to 0\} (\sin(\tan x) - \tan(\sin x))/(\sin^{-1}(\tan^{-1}x) - \tan^{-1}(\sin^{-1}x)) = 25.2(1994)159$ 

498.

Proposer: David Callan 24.2(1993)184

Topic: Find row sums in a Pascal-like triangle Solution: A Pascal-like triangle 25.2(1994)161

499.

Proposer: Frank Schmidt 24.2(1993)184

Topic: Do there exist an infinite number of finite graphs satisfying 3 given conditions?

Solution: An infinite class of planar graphs 25.2(1994)162

500.

Proposer: Michael Fatliff 24.2(1993)184

Topic: Inequalities involving partial quotients of simple continued fractions

Solution: An ordering of partial quotients 25.2(1994)163

501.

Proposer: K. R. S. Sastry 24.3(1993)271

Topic: Necessary & sufficient condition that the semi-perimeter of a right triangle is a

triangular number

Solution: A Triangle Semi-Perimeter 25.3(1994)241

502.

Proposer: Zhang Zaiming 24.3(1993)271

Topic: Finding values that guarantee the equality of 2 sums of integers

Solution: Pell's equation - once again 25.3(1994)241

503.

Proposer: Louis R. Bragg & Jerrold W. Grossman 24.3(1993)271

Topic: Finding the different triangles with limited integral length of sides

Solution: Counting "Diophantine" triangles 25.3(1994)243

Proposer: Gloria Olive 24.3(1993)272

Topic: Expressing products of primes as the sum of consecutive positive integers

Solution: Factorizations and sums 25.3(1994)244

505.

Proposer: Parviz Khajeh-Khalili 24.3(1993)272

Topic: Show that a sequence of logarithms is decreasing and find its limit

Solution: Area above and below a hyperbola 25.3(1994)245

506

Proposer: Heinz-Jürgen 24.4(1993)377

Topic: Equality of 2 sums, one involving products of sums

Solution: A sum of a product of a sum and a product 25.4(1994)335

507.

Proposer: Jiro Fukuta 24.4(1993)377

Topic: Inequality involving the lengths of sides of a quadrilateral

Solution: An inequality for the perimeter of a quadrilateral 25.4(1994)336

508.

Proposer: K. R. S. Sastry 24.4(1993)377

Topic: Find all Pythagorean triangles with n-gonal sides and a common rank

Solution: Polygonal Pythagorean triples 25.4(1994)337

509.

Proposer: Norman Schaumberger 24.4(1993)378 Topic: Diophantine equation in 5 variables

Solution: A Diophantine equation with successive powers 25.4(1994)338

510.

Proposer: Murray S. Klamkin 24.4(1993)378

Topic: Comparing 2 multiple integrals of sines and cosines Solution: Trigonometric integral inequalities 25.4(1994)338

511.

Proposer: Zhang Zaiming 24.5(1993)472

Topic: Inequality involving the sides and areas of 2 triangles Solution: An inequality for two triangles 25.5(1994)463

512.

Proposer: Richard Carpenter & Homer White 24.5(1993)472

Topic: Find the determinant of a given matrix

Solution: A determinant of subscript products 25.5(1994)464

513.

Proposer: Frank J. Flanigan 24.5(1993)473

Topic: Finding the constant term guaranteeing a cubic equation has 3 integral roots

Solution: Cubics with no integer roots 25.5(1994)465

514.

Proposer: David Doster 24.5(1993)473

Topic: Finding the limit of a sequence of quotients of 2 other sequences

Solution:  $\lim \{\text{from } n \to \infty\} \ p_n / q_n = \sqrt[3]{2} \ 25.5(1994)465$ 

Proposer: Larry Hoehn 24.5(1993)473

Topic: Necessary & sufficient condition that a given quadrilateral is a parallelogram

Solution: A parallelogram characterization 25.5(1994)466

516.

Proposer: Ioan Sadoveanu 25.1(1994)64

Topic: Given the roots of one polynomial, solve another Solution: Roots of related polynomials 26.1(1995)67

517.

Proposer: Kazem S. Sadati 25.1(1994)64

Topic: If squared sides of a triangle are in arithmetic progressions, so are the cotangents

Solution: Cotangents in arithmetic progression 26.1(1995)68

518.

Proposer: K. R. S. Sastry 25.1(1994)64

Topic: Find a triple of triangular numbers analogous to a Pythagorean triple and having a

Sum also a triangular number

Solution: Pythagorean triples of triangular numbers 26.1(1995)69

519.

Proposer: Jane Friedman 25.1(1994)65

Topic: Express even powers of Fibonacci numbers as a linear combination of Lucas numbers

Solution: A linear combination of Lucas numbers 26.1(1995)70

520.

Proposer: Murray S. Klamkin 25.1(1994)65

Topic: Determine all positive integer pairs satisfying certain geometric progressions

Solution: Integer-valued geometric progressions 26.1(1995)71

521.

Proposer: Ioan Sadoveanu 25.2(1994)157

Topic: Show a polynomial is constant given a root of another polynomial

Solution: A constant polynomial 26.2(1995)158

522.

Proposer: Frank Schmidt 25.2(1994)157

Topic: Find the average weight of a vector over all bases in a vector space

Solution: Averaging vector weights 26.2(1995)159

523.

Proposer: Edward T. H. Wang 25.2(1994)157

Topic: Find all natural numbers satisfying a binomial coefficient divisibility requirement

Solution: Divisibility of binomial coefficients 26.2(1995)160

524.

Proposer: Norman Schaumberger 25.2(1994)158
Topic: Inequalities involving 3 positive numbers
Solution: The a, b, c's of inequalities 26.2(1995)161

Proposer: Edwin Buchman 25.2(1994)158

Topic: Probability involving eating 2 kinds of candy Solution: Probabilities for a candy jar 26.2(1995)162

526.

Proposer: Frank Schmidt 25.3(1994)240

Topic: Inequalities involving a real symmetric idempotent matrix

Solution: Bounds for matrix sums 26.3(1995)245

527.

Proposer: Murray S. Klamkin 25.3(1994)240

Topic: Find the minimum degree of a 4-variable polynomial with a divisibility criterion

Solution: The minimum degree of a symmetric polynomial 26.3(1995)246

528.

Proposer: Gloria Olive 25.3(1994)240

Topic: Evaluating a sum involving Stirling numbers of the first kind

Solution: A Stirling series for 1/x 26.3(1995)246

529.

Proposer: Jiro Fukuta 25.3(1994)241

Topic: Find the locus of points of an interior point to a rectangle with distance requirements

Solution: Hyperbola in a rectangle 26.3(1995)248

530.

Proposer: K. R. S. Sastry 25.3(1994)241

Topic: Find an integer depending of a multiple of its 4 proper divisors

Solution: An equality for divisors 26.3(1995)249

531.

Proposer: Murray S. Klamkin 25.4(1994)334

Topic: Given 3 angles between consecutive vertices of a quadrilateral, find the 4th

Solution: Solving a quadrilateral 26.4(1995)330

532.

Proposer: Mike Chamberlain & Mark D. Meyerson 25.4(1994)334

Topic: Finding the maximum distance between a viewer and a tilted billboard

Solution: Tilting of billboards 26.4(1995)331

533.

Proposer: K. R. S. Sastry 25.4(1994)334

Topic: Find all natural numbers having the product of the sum of the first n squares and the

next n squares which yield a perfect square

Solution: Square products of sums of squares 26.4(1995)333

534.

Proposer: Broderick Oluyede 25.4(1994)335

Topic: Inequality involving products of sums of 2 sequences of positive numbers

Solution: An inequality for positive sums 26.4(1995)333

Proposer: Harry Sedlinger 25.4(1994)335

Topic: There exist an infinite number of right triangles whose semi-perimeter is triangular

Solution: Triangular semi-perimeters ad infinitum 26.4(1995)334

536.

Proposer: Murray S. Klamkin 25.5(1994)462

Topic: Finding minimum values of algebraic expressions involving 4 positive numbers

Solution: Three minima, with constraints 26.5(1995)406

537.

Proposer: Herbert Gülicher 25.5(1994)462

Topic: Concurrency of lines involving the cevian and distances in a triangle

Solution: Concurrent constructions 26.5(1995)407

538.

Proposer: Murray S. Klamkin 25.5(1994)462

Topic: Maximum area of a quadrilateral given angles between consecutive vertices

Solution: The maximum area of a quadrilateral 26.5(1995)407

539.

Proposer: Neven Jurić 25.5(1994)463

Topic: Number of ways to form equilateral triangles in an n-dimensional cube

Solution: Equilateral triangles in a cube 26.5(1995)409

540.

Proposer: Stephen Penrice 25.5(1994)463

Topic: Limit involving the expected position of a numbered ball in a permutation

Solution: An urn model for permutations 26.5(1995)410

541.

Proposer: Victor Oxman 26.1(1995)66

Topic: Constructing a line tangent to an ellipse from a point on a line off the ellipse

Solution: Tangent ellipses 27.1(1996)75

542.

Proposer: Jorge-Nuno O. 26.1(1995)66

Topic: Congruence identity involving Euler's totient function

Solution: Summing powers mod m 27.1(1996)75

543.

Proposer: K. R. S. Sastry 26.1(1995)66

Topic: Necessary & sufficient condition that 2 parallelograms are congruent

Solution: Congruent self-diagonal parallelograms 27.1(1996)76

544.

Proposer: Murray Klamkin 26.1(1995)67

Topic: Evaluate a finite sum of polynomials divided by factorials Solution: An easy sum? No, just easily summed 27.1(1996)77

Proposer: Jiro Fukuta 26.1(1995)67

Topic: Necessary & sufficient condition for the existence of a quadrilateral that admits a

Circumcircle

Solution: An inscribed quadrilateral 27.1(1996)78

546.

Proposer: K. R. S. Sastry 26.21(1995)157

Topic: Prove that a certain triangle is isosceles

Solution: An isosceles triangle problem 27.2(1996)150

547.

Proposer: Curtis Cooper & Robert E. Kennedy 26.2(1995)157

Topic: Identities involving the gcd and lcm of 2 numbers and the order of 10 mod k

Solution: Order mod 10 27.2(1996)150

548.

Proposer: Michael Golumb 26.2(1995)157

Topic: Necessary & sufficient condition for a unique square circumscribing a parallelogram

Solution: Circumscribing a square about a parallelogram 27.2(1996)151

549.

Proposer: Alta Kellogg 26.2(1995)158

Topic: Are there any graphs which are both self-complementary and self-dual?

Solution: Self-dual and self-complementary graphs 27.2(1996)152

550.

Proposer: Norman Schaumberger 26.2(1995)158

Topic: Evaluate the sum of a series of reciprocals of products of 3 odd integers

Solution: A Sum of (ln 3) /16 27.2(1996)154

551.

Proposer: K. R. S. Sastry 26.3(1995)244

Topic: The median of a Heronian triangle does not equal the length of any side

Solution: An impossibility result for Heronian triangles 27.3(1996)232

552.

Proposer: Hongwei Chen & Parviz Khajeh-Khalili 26.3(1995)244 Topic: Find all C<sup>2</sup> functions satisfying a given functional equation

Solution: A functional equation of quadratics 27.3(1996)232

553.

Proposer: Michael Golumb 26.3(1995)244

Topic: The sum of projections from a certain n-gon to a line is independent of the line

Solution: Invariant projections 27.3(1996)233

554.

Proposer: Juan-Bosco Romero Márquez 26.3(1995)244

Topic: Bounds for the nth root of the product of row sums of a matrix Solution:

Bounds for a matrix row-sum product 27.3(1996)234

Proposer: Can Anh Minh 26.3(1995)245

Topic: Upper bound for a product and a sum involving the 1<sup>st</sup> 1995 integers

Solution: Last year's inequality 27.3(1996)235

556.

Proposer: Frank Schmidt 26.4(1995)329

Topic: Find a matrix whose product with its transpose is a multiple of the identity matrix

Solution: Orthogonal-like matrices 27.4(1996)313

557.

Proposer: K. R. S. Sastry 26.4(1995)329

Topic: Find primitive Pythagorean triangles sharing properties with (3,4,5) and (5,12,13)

Solution: A plethora of pairs of primitive Pythagorean triples 27.4(1996)314

558.

Proposer: Jiro Fukuta 26.4(1995)329

Topic: For any triangle only one triplet has distances from vertices obeying 3 conditions

Solution: A corollary of Ceva's theorem 27.4(1996)315

559.

Proposer: Richard Johnsonbaugh 26.4(1995)329 Corrected: 27.4(1996)315 Topic: Necessary & sufficient condition for denominations of coins of be orderly

Solution: Orderly currencies 28.4(1997)316

560.

Proposer: Filip Sajdak 26.4(1995)330

Topic: Inequality involving 1995 and the 3 number theoretic functions  $\sigma(n)$ ,  $\tau(n)$ , and  $\pi(n)$ 

Solution: An inequality with three arithmetic functions 27.4(1996)316

561.

Proposer: Carlton Kellog 26.5(1995)405

Topic: Convergence of a sequence of reciprocals of Euler's totient function Solution: Must  $\Sigma 1/\varphi(a_n)$  converge when  $\Sigma 1/a_n$  converges? 27.5(1996)405

562.

Proposer: Murray S. Klamkin 26.5(1995)405

Topic: Evaluation of a given  $(n + 2) \times (n + 2)$  symmetric determinant

Solution: A symmetric determinant 27.5(1996)406

563.

Proposer: Frank Schmidt 26.5(1995)405

Topic: Finding coefficients for surjective functions of 2 and 3 variables

Solution: Linear combinations of squares 27.5(1996)407

564.

Proposer: Can Anh Minh 26.5(1995)406

Topic: Condition that a convex quadrilateral is cyclic or a trapezoid

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Proposer: K. R. S. Sastry 26.5(1995)406

Topic: Find a rectangular box with volume equaling the sum of the edges and surface area

Solution: New perfect boxes 27.5(1996)408

566.

Proposer: K. R. S. Sastry 27.1(1996)74

Topic: Integral coefficients in a cubic yielding linear factors with integral coefficients

Solution: A characterization for integral roots 28.1(1997)68

567.

Proposer: Heinz-Jürgen Seiffert 27.1(1996)74

Topic: Inequalities in two variables involving the hyperbolic sine function

Solution: An hyperbolic sine mean 28.1(1997)69

568.

Proposer: Frank Schmidt 27.1(1996)74

Topic: Characterize all bipartite graphs with chromatic polynomials having real roots

Solution: Trees have real roots? 28.1(1997)70

569.

Proposer: Can Anh Minh 27.1(1996)75

Topic: Upper bound for the largest denominator in a unit sum of unit fractions

Solution: A maximum denominator 28.1(1997)71

570.

Proposer: Murray S. Klamkin 27.1(1996)75

Topic: A triangle with angle bisectors intersecting an altitude is isosceles

Solution: An isosceles triangle problem - again 28.1(1997)72

571.

Proposer: Frank Schmidt 27.2(1996)149

Topic: Find all cyclotomic polynomials whose coefficients are all nonzero Solution: Cyclotomic polynomials with nonzero coefficients 28.2(1997)146

572.

Proposer: George Baloglou 27.2(1996)149 Topic: Trigonometric - hyperbolic inequality

Solution:  $\tanh \theta \le \tan \theta$  for  $-\pi/4 < \theta < \pi/4$  28.2(1997)147

573.

Proposer: Lewis Lum 27.2(1996)149

Topic: Congruence classes for a set with subset members having sums never congruent to 0

Solution: Restricted sums modulo n 28.2(1997)148

574.

Proposer: Robert Patenaude 27.2(1996)149

Topic: Locus of the foci of an ellipse inscribed in a non-square rectangle

Solution: The loci of foci 28.2(1997)148

Proposer: Parviz Khajeh-Khalili 27.2(1996)149

Topic: Identity involving sums and the Riemann zeta function

Solution: Zeta sums 28.2(1997)149

576.

Proposer: Peter Daffer 27.3(1996)231

Topic: Convergence of a sum of n-fold compositions of a function with itself

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577.

Proposer: K. R. S. Sastry 27.3(1996)231

Topic: Identity involving the vertices and angles of a convex heptagon

Solution: Ratios in a right heptagon 28.3(1997)233

578.

Proposer: Robert Patenaude 27.3(1996)231

Topic: Find the lengths of the sides of a given triangle

Solution: Triangles with one angle twice another 28.3(1997)233

579.

Proposer: Juan Ryan & Steve Pennell 27.3(1996)231

Topic: Find the line minimizing the sum of distances to the line from 3 given points

Solution: Least absolute deviation 28.3(1997)235

580.

Proposer: M. L. Glasser 27.3(1996)232

Topic: Definite integral involving the logarithm function Solution: An integral whose value is  $(\ln 2)^2 / n$  28.3(1997)235

581.

Proposer: Farshid Arjomandi 27.4(1996)312

Topic: Solve a system of equations in n variables Solution: A system of power equations 28.4(1997)317

582.

Proposer: Can A. Minh 27.4(1996)312

Topic: Evaluate the limit of a sum depending on sines Solution: A sine series with a linear limit 28.4(1997)318

583.

Proposer: Murray Klamkin 27.4(1996)312

Topic: Is a parabola the only curve satisfying a property about tangents to the curve?

Solution: A characterization of parabolas 28.4(1997)319

584.

Proposer: Monte J. Zerger 27.4(1996)313

Topic: Find rationals with product of numerator and denominator repeating in its decimal

Solution: A characterization of 1/3 and 2/3 28.4(1997)320

Proposer: K. R. S. Sastry 27.4(1996)313

Topic: Triangles with relatively prime sides and one side square and another nonintegral

Solution: Triangles with relatively prime sides 28.4(1997)321

586.

Proposer: K. R. S. Sastry 27.5(1996)404

Topic: A triangle must be equilateral if one formed by extending its sides is also

Solution: Triangles within triangles 28.5(1997)407

587.

Proposer: Herbert Gülicher 27.5(1996)404

Topic: Necessary & sufficient condition that the determinant of a given matrix is zero

Solution: A determinant of mostly 1's 28.5(1997)408

588.

Proposer: Can A. Minh 27.5(1996)404

Topic: Inequality involving the cotangents of the angles of a triangle

Solution: Squared tangents 28.5(1997)408

589.

Proposer: Tom Farmer 27.5(1996)404

Topic: A given harmonic sequence must be dense and contain no integers

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590.

Proposer: F. Sajdak 27.5(1996)405

Topic: Inequality involving the cardinality of a set of number theoretic functions

Solution: Many n's with  $(\varphi(n), \tau(n), \sigma(n)) = 1 28.5(1997)410$ 

591.

Proposer: Wu Wei Chao 28.1(1997)67

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592.

Proposer: F. J. Flanigan 28.1(1997)67

Topic: Find complex functions with an infinite number of balanced values

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593.

Proposer: James Duemmel 28.1(1997)68

Topic: Probability that the eigenvalues of a real  $2 \times 2$  matrix are nonreal

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594.

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Topic: Validity of an algebraic inequality Solution: A binomial inequality 29.1(1998)70

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Topic: Limit of the ratio of differences of 2 medians and 2 angle bisectors of a triangle

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596.

Proposer: David Doster 28.2(1997)145

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Solution: Counting odd divisors of odd integers 29.2(1998)153

597.

Proposer: Murray S. Klamkin 28.2(1997)145

Topic: Find linear functions divisible by 19 given linear function of their coefficients

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598.

Proposer: Kenichiro 28.2(1997)145

Topic: Evaluate the sum of powers of some of the roots of unity Solution: From roots of unity to the Möbius function 29.2(1998)154

599.

Proposer: Juan-Bosco Romeo Márquez 28.2(1997)145

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600.

Proposer: Georgia M. Benkart, Mark D. Meyerson & William P. Wardlaw 28.2(1997)146 Topic: Prove that there may or may not be an invertible element in a certain ring with 1

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Proposer: William P. Wardlaw 28.3(1997)231

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602.

Proposer: Yi-chuan Pan 28.3(1997)231

Topic: Prove that a sequence formed from Pell numbers is always square

Solution: A Pell sequence of squares 29.3(1998)244

603.

Proposer: Juan-Bosco Romeo Márquez 28.3(1997)231

Topic: Inequalities involving n<sup>th</sup> roots of ratios of functions of 2 positive numbers

Solution: Consequences of convexity 29.3(1998)245

604.

Proposer: Jiro Fukuta 28.3(1997)231

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Proposer: A. P. Stone 28.3(1997)232

Topic: Find nearly isosceles Pythagorean quadruples

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606.

Proposer: G. Trenkler, S. O. Troschke & J. Gross 28.4(1997)315

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607.

Proposer: Noah Rosenberg 28.4(1997)315

Topic: Describing a set of points on a sequence of convex m-gons

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608.

Proposer: Daniel E. Penney 28.4(1997)315

Topic: Determining convergence of an arrangement of the alternating harmonic series

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609.

Proposer: Peter Schumer 28.4(1997)316

Topic: Existence of a number modulo a prime p which is the sum of 2 squares

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610.

Proposer: Ken Korbin 28.4(1997)316

Topic: Finding 3 term polynomials divisible by a given quadratic

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611.

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Topic: Find the arithmetic mean of the zeroes of a rational function

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612.

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Topic: Find a function whose graph has a tangent of unit length in the first quadrant

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613.

Proposer: Michael Scott McClendon 28.5(1997)406

Topic: Find the length of an altitude in an isosceles triangle with unit inradius

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614.

Proposer: Peter Schumer 28.5(1997)406

Topic: Are there many consecutive positive integers not expressible as a sum of squares?

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Proposer: Western Maryland College Problem Group 28.5(1997)407

Topic: Find points on and off an ellipse related to tangent lines from a given point

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616.

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Topic: Comparing areas in regions enclosed by convex curves Solution: Quadrants in closed convex curves 30.1(1999)61

617.

Proposer: Kenichiro Kashihara 29.1(1998)66

Topic: Solving a Diophantine equation with one variable an exponent

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618.

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Topic: Inequality involving alternating reciprocals of factorials

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619.

Proposer: Götz Trenkler 29.1(1998)66

Topic: Finding a generalized inverse of a quasi-idempotent matrix

Solution: A generalized inverse for quasi-idempotent matrices 30.1(1999)65

620.

Proposer: Sam Speed 29.1(1998)67

Topic: Find the minimum value of the number of partitions of n added to its maximum

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621.

Proposer: Jedd Beall, Lenny Jones, Mike Seyfried & Kathryn Seyfried 29.2(1998)152

Topic: Find positive integer pairs with the square of one's digit sums equal the other integer

Solution: Squares as sums of digits 30.2(1999)144

622.

Proposer: Michael Golumb 29.2(1998)152

Topic: Properties about the number of beads distributed at the vertices of an n-gon

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623.

Proposer: Alexander Kheyfits 29.2(1998)152

Topic: Evaluating a double sum of reciprocals of integers > 1

Solution: A series whose sum is ln k 30.2(1999)145

624.

Proposer: Harry Sedinger 29.2(1998)153

Topic: Existence of a point which maximizes the angle made from it to 2 points on a line

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Proposer: Sining Zheng & Yuyue Song 29.2(1998)153

Topic: Finding power series having the radius of convergence of another power series

Solution: Extending the radius of congruence 30.2(1999)147

626.

Proposer: Juan Mártin Mombelli 29.3(1998)242

Topic: Equation involving the number theoretic functions  $\tau(n)$ ,  $\sigma(n)$  and  $\phi(n)$ 

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627.

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628.

Proposer: Frank Schmidt 29.3(1998)242

Topic: Find n so that the symmetric group  $S_n$  is a subgroup of GL(2,n)

Solution: Embedding  $S_n$  in GL(2,p) 30.3(1999)232

629.

Proposer: David Beran 29.3(1998)242

Topic: Conditions on 2 angle bisectors of a triangle which guarantees it being isosceles

Solution: An isosceles triangle 30.3(1999)233

630.

Proposer: Michael Andreoli 29.3(1998)243

Topic: Expected number of corrected guesses in a card game

Solution: Guessing card colors 30.3(1999)234

631.

Proposer: K. R. S. Sastry 29.4(1998)330

Topic: Finding an odd integer which shares certain properties enjoyed by the integer 5

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632.

Proposer: Frank Schmidt 29.4(1998)330

Topic: Finding graphs which share certain properties enjoyed by a pentagon Solution: A 4-regular, 3-chromatic, self-complementary graph 30.4(1999)320

633.

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634.

Proposer: Juan Mártin Mombelli 29.4(1998)331 Topic: Solving a 2 variable functional equation

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Topic: Sums of squares of chords forming a right angle with a point inside a circle

Solution: Orthogonal chords in a circle 30.4(1999)323

636.

Proposer: K. R. S. Sastry 29.5(1998)434

Topic: Identity involving the number and sum of unitary divisors of natural numbers

Solution: A convolving sum 30.5(1999)407

637.

Proposer: Doug Ensley 29.5(1998)434

Topic: Finding the limit of a sequence of square roots Solution: A quadratic recursion limit 30.5(1999)408

638.

Proposer: Manjul Bhjargava 29.5(1998)434

Topic: Evaluate the sum of reciprocals of binomial coefficients

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639.

Proposer: Alan H. Rapoport 29.5(1998)435

Topic: Number of ways of aligning 25 people by height in a  $5\times5$  matrix array

Solution: A square Young tableau 30.5(1999)410

640.

Proposer: Michael Golumb 29.5(1998)435

Topic: Inequality involving non-square integers whose square begins with the integer

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641.

Proposer: Arthur L. Holshouser 30.1(1999)60

Topic: Finding functions with graphs satisfying properties about line symmetries

Solution: From one symmetry many 31.1(2000)63

642.

Proposer: Kwnichiro Kashihara 30.1(1999)60

Topic: Diophantine-type equation involving powers as sums of factorials

Solution: A sum of factorials 31.1(2000)65

643.

Proposer: William F. Trench 30.1(1999)60

Topic: Finding limits of sequences defined by double sums of a given positive sequence

Solution: Two double sums 31.1(2000)65

644.

Proposer: Lawrence Spence and Charles Vanden Eynden 30.1(1999)61

Topic: Finding certain polynomials expressible as the product of 2 such polynomials

Solution: Products of polynomials 31.1(2000)64

Proposer: James Graham-Eagle 30.1(1999)61

Topic: Summing a series of terms from a logarithm sequence for odd integers

Solution: Stirling's approximation to the rescue 31.1(2000)67

646.

Proposer: Parviz Khalili 30.2(1999)143

Topic: Necessary & sufficient condition that the graph of a 5<sup>th</sup> degree polynomial has a point

of symmetry

Solution: Quintic symmetry 31.2(2000)138

647.

Proposer: K. R. S. Sastry 30.2(1999)143

Topic: Number of triangles having certain properties on the area and sides of the triangle

Solution: A family of Heron triangles 31.2(2000)139

648.

Proposer: Ayoub B. Ayoub 30.2(1999)143

Topic: Condition for which an integer exists guaranteeing a Pythagorean triple

Solution: A family of Pythagorean triples 31.2(2000)140

649.

Proposer: Todd Will 30.2(1999)144

Topic: Existence of "power special" sequences of non-integer reals

Solution: Power special sequences 31.2(2000)138

650.

Proposer: Kenneth Korbin 30.2(1999)144

Topic: Express the side of a triangle in terms of radii of 2 inscribed circles

Solution: Radii of inscribed circles 31.2(2000)142

651.

Proposer: Frank Schmidt 30.3(1999)230

Topic: Existence of 3 matrices with trace > 0 having mutual products with trace < 0

Solution: Trace conditions 31.3(2000)220

652.

Proposer: Seth Zimmerman 30.3(1999)230

Topic: Maximum number of points in a plane with any 3 having 2 one unit apart

Solution: A graph in the plane 31.3(2000)221

653.

Proposer: Răzvan Tudoran 30.3(1999)230

Topic: Recurring sequence with the n<sup>th</sup> term divisible by the n<sup>th</sup> prime

Solution: A well known sequence 31.3(2000)223

654.

Proposer: Ice B. Risteski 30.3(1999)230

Topic: Dimensions of subspaces of a vector space over various fields Solution: The dimension of a subspace over different fields 31.3(2000)224

Proposer: Charles Vanden Eynden 30.3(1999)231

Topic: Finding values which guarantee a graph has a Hamilton circuit

Solution: A Hamiltonian circuit on a box 31.3(2000)225

656.

Proposer: Frank Schmidt 30.4(1999)318

Topic: Convergence of a sum and other properties of a sequence of integrals

Solution: A sequence of integrals 31.4(2000)316

657.

Proposer: Zengxiang Tong 30.4(1999)318

Topic: Primes that divide the numerator of finite sums of the alternating harmonic series

Solution: A divisibility relation in the alternating harmonic series 31.4(2000)317

658.

Proposer: Roger B. Nelsen 30.4(1999)318

Topic: Possible independence criteria for random variables

Solution: Independence and squaring 31.4(2000)318

659.

Proposer: Pete Johnson & Dave Leach 30.4(1999)319

Topic: GCD of the powers of a polynomial with a unique real root

Solution: The roots of a polynomial equation 31.4(2000)318

660.

Proposer: Ho-joo Lee 30.4(1999)319

Topic: Coefficient of a cubic equation which allows a certain complex root

Solution: A consequence of FLT 31.4(2000)319

661.

Proposer: Michael S. McClendon 30.5(1999)406

Topic: Ladder problem of calculus turning a non-rectangular corner

Solution: Angled hallway ladder problem 31.5(2000)409

662.

Proposer: Bradley A. Warner & Bradford Kline 30.5(1999)407

Topic: Probability and expected value of number of rounds and flips in a coin tossing game

Solution: Probabilities and expected values in a coin tossing game 31.5(2000)410

663.

Proposer: Mizan R. Khan 30.5(1999)407

Topic: Roots and number of roots of a bracket function equation of the gcd of 2 variables

Solution: Solving a ceiling equation 31.5(2000)411

664.

Proposer: Jiro Fukuta 30.5(1999)407

Topic: The incenter is collinear with and is the midpoint of radical centers in a triangle

Solution: The incenter as an average of radical centers 31.5(2000)413

Proposer: Kenneth Korbin 30.5(1999)407

Topic: Smallest positive integer which is the sum of 2 triangular numbers in 48 ways

Solution: Sums of triangular numbers 31.5(2000)4104

666.

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Topic: Probabilities in the Car and Goat problem Solution: Cars and goats revisited 32.1(2001)61

667.

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Topic: Integrally dependent integral of a ratio of cosine functions

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668.

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Topic: Prime numbers satisfying a 4-variable equation Solution: A Diophantine equation with tens 32.1(2001)63

669.

Proposer: Lance E. Hemlow 31.1(2000)63

Topic: Properties relating to an indefinite arc length integral Solution: Parametrizing some arclength integrals 32.1(2001)64

670.

Proposer: Juan-Bosco Romero Márquez 31.1(2000)63

Topic: Limit of an algebraic ratio involving the length of an angle bisector in a triangle Solution: A limiting comparison of an angle bisector and an altitude 32.1(2001)67

671.

Proposer: Arthur L. Holshouser 31.2(2000)137

Topic: A subgroup in a nested sequence is almost normal to super groups in the nest

Solution: Almost normal subgroups 32.2(2001)142

672.

Proposer: K. R. S. Sastry 31.2(2000)137

Topic: Necessary & sufficient condition that the Gergonne point of a triangle's cevians be a

midpoint

Solution: A Gergonne midpoint 32.2(2001)143

673.

Proposer: Zengxiang Tong 31.2(2000)137

Topic: Finding a power of 2 making a sum of powers of 2 a perfect square

Solution: A Diophantine equation with twos 32.2(2001)144

674.

Proposer: Roger B. Nelsen 31.2(2000)138

Topic: Probability, uniform distribution and triangle density of continuous random variables

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Proposer: Monte J. Zerger 31.2(2000)138

Topic: Range of a sum of arctangents defined on a specific set depending on 3 variables

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676.

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677.

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678.

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Topic: Find a double finite sum of a sequence as a function of its largest subscript

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679.

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Topic: Probabilities of obtaining various amounts of 2's and 0's from a set of 2's and 0's

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680.

Proposer: Kent Holing 31.3(2000)220

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given area quantity

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682.

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Topic: Optimal path for one moving particle in a plane to reach a point before another

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684.

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Topic: Ratios of lengths in a configuration of triangles Solution: Ratios of areas and lengths 32.4(2001)301

Proposer: Mario Martelli 31.4(2000)316

Topic: Values that guarantee finite positive limits in a sequence of definite integrals

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686.

Proposer: K. R. S. Sastry 31.5(2000)408

Topic: Questions concerning lengths of sides of FFF-triangles

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687.

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688.

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Topic: Characterize sequences having a given limit to a sequence of roots of a polynomial

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689.

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Topic: Any bounded metric space can be embedded in an antipodal metric space

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690.

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Topic: Double sum of squared binomial coefficients

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700.

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Topic: Existence of polynomials with given properties

Solution: Polynomial fit 33.5(2002)411

712.

Proposer: Stan Lipovetsky 32.5(2001)381

Topic: Find number bases b allowing an even self-enumerating base b integer

Solution: Self-enumerating base b integers 33.5(2002)412

713.

Proposer: Parviz Khalili 32.5(2001)382

Topic: Limit of the ratio of the areas of 2 triangles formed from points on the graph of y=x<sup>n</sup>

Solution: Limiting ratios of areas 33.5(2002)413

714.

Proposer: Arthur L. Holshouser & Harold B. Reiter 32.5(2001)382

Topic: Adapting strategies in the game of Blocking Nim

Solution: Blocking Nim 33.5(2002)414

Proposer: M. N. Deshpande 32.5(2001)382

Topic: Equality of products of distances from lines constructed in a triangle

Solution: A triangle identity 33.5(2002)416

716.

Proposer: Cecelia A. Weajley & William D. Weakley 33.1(2002)54

Topic: Uniquely determined values of a function defined on sets of real numbers

Solution: Reminiscent of inclusion-exclusion 34.1(2003)69

717.

Proposer: Erwin Just 33.1(2002)54

Topic: Find an increasing finite set of integers each dividing the sum of squares of each one

Solution: Divisibility and sums of powers 34.1(2003)70

718.

Proposer: Norman Schaumberger 33.1(2002)54

Topic: Inequality involving ratios and powers of 2 positive numbers > 1

Solution: An application of concavity 34.1(2003)70

719.

Proposer: Wu WeiChao 33.1(2002)55

Topic: Necessary & sufficient condition that a function satisfies a 2-variable given equation

Solution: A projection in disguise 34.1(2003)71

720.

Proposer: Andrew Cusumano 33.1(2002)55

Topic: Limit of the difference of 2 ratios of sequences of integers

Solution: Not an easy "e" asy limit

721.

Proposer: Kent Holing 33.2(2002)150

Topic: Necessary & sufficient condition that a quadrilateral related to a triangle is cyclic

Solution: Untitled 34.2(2003)154

722.

Proposer: Juan-Bosco Romero Márquez 33.2(2002)150

Topic: A function of x depends on 3 exponents. Find values of the 3 that will guarantee a

right or left hand limit of the function as x approaches 1, and find the limit.

Solution: Untitled 34.2(2003)155

723.

Proposer: David Bloom 33.2(2002)150

Topic: Proving certain properties of a given ring with unity

Solution: Untitled 34.2(2003)156

724.

Proposer: Wu Wei Chao 33.2(2002)151

Topic: Find a geometric characterization that a given sequence is periodic

Solution: Untitled 34.2(2003)157

Proposer: Andrew Cusumano 33.2(2002)151

Topic: Find the limit of a sum as a function of the number of terms summed

Solution: Untitled 34.2(2003)158

726.

Proposer: Thomas J. Pfaff 33.3(2002)240

Topic: Limit of a summation sequence of cosecants if it exists

Solution: A limit involving the  $x/\sin(x)$  approximation 34.3(2003)240

727.

Proposer: Yves Nievergelt 33.3(2002)240

Topic: Rank 4 terms involving 2 variables in increasing order

Solution: Rational function inequalities 34.3(2003)241

728.

Proposer: Erwin Just 33.3(2002)240

Topic: Determining weights of coins in identical bags Solution: A coin-weighing problem 34.3(2003)242

729.

Proposer: Roger B. Nelsen 33.3(2002)241

Topic: Inequality for the mean and standard deviation of a concave up survival function

Solution: A consequence of convexity 34.3(2003)243

730.

Proposer: Jerome Minkus 33.3(2002)241

Topic: Properties relating to a triangle with a trisected angle

Solution: Similarity invariants for an angle trisection 34.3(2003)244

731.

Proposer: Michael Scott McClendon 33.4(2002)325

Topic: Find the volume of airspace for a plane attached to a spherical planet

Solution: The airspace of a tethered airplane 34.4(2003)328

732.

Proposer: Ron Rietz 33.4(2002)325

Topic: Inequalities for a logarithmic function and summing the digits in a decimal

Solution: Not quite an integer 34.4(2003)329

733.

Proposer: William Seaman 33.4(2002)325

Topic: Existence of a 1-1 function defined on certain subsets of n elements

Solution: A marriage of sets 34.4(2003)330

734.

Proposer: Michael Bataille 33.4(2002)326

Topic: Find the gcd's of consecutive terms in recursive sequences Solution: Greatest common divisors in linear recurrence 34.4(2003)331

Proposer: Norman Bolton 33.4(2002)326

Topic: Probability that n persons with assigned seats sit in the correct one

Solution: Finding the right seat 34.4(2003)332

736.

Proposer: Samuel A. Truitt, Jr. 33.5(2002)410

Topic: Describe sets of values that satisfy a sine and those that satisfy a cosine equation

Solution: Special cases of angle sum formulas 34.5(2003)406

737.

Proposer: Thomas J. Pfaff 33.5(2002)410

Topic: Can a complete graph be partitioned into edge disjoint paths? Solution: Yet another proof that  $1 + 2 + \dots + (n - 1) = C(n,2)$  34.5(2003)408

738.

Proposer: Nora Thornber 33.5(2002)411

Topic: Initial value problem for an n-dimensional vector function

Solution: An initial value problem 34.5(2003)408

739.

Proposer: Arthur L Holshouser 33.5(2002)411

Topic: Winning strategies for a counter removing game Solution: Strategies in a two-person game 34.5(2003)409

740.

Proposer: Richard F. McCoart, Jr. 33.5(2002)411

Topic: Perturbing the birth dates of Niels Bohr and Werner Heisenberg

Solution: Not just another Bohring question 34.5(2003)410

741.

Proposer: Karl Havlak & Charles Diminnie 34.1(2003)68 Topic: Limits of 2 sequences of ratios of positive numbers

Solution: A pair of similar limits 35.1(2004)56

742.

Proposer: Harris Kwong 34.1(2003)68

Topic: Inequality involving polynomial sequences Solution: A polynomial inequality 35.1(2004)57

743.

Proposer: Najib N. Yazbak 34.1(2003)68 Topic: System of 2 equations in 3 variables

Solution: Exponential Diophantine equations 35.1(2004)58

744.

Proposer: Vassilios C. Hombas 34.1(2003)69

Topic: Evaluating a function with 2<sup>nd</sup> derivatives appearing in a converging sum at 1

Solution: A functional equation 35.1(2004)59

Proposer: Rex H. Wu 34.1(2003)69

Topic: Divisibility and cardinality of a function yielding prime values

Solution: Dividing m! But not (m - 1)! Revisited 35.1(2004)56

746.

Proposer: Emily Just & Erwin Just 34.2(2003)153

Topic: Existence of an integer from sums of integers assigned to n-gon mid and end points

Solution: There are no magic (2n + 1)-gons 35.2(2004)137

747.

Proposer: Josè Luis Díaz-Barrero 34.2(2003)153 Topic: Fibonacci number summation inequality

Solution: An inequality with Fibonacci numbers 35.2(2004)138

748.

Proposer: Kent Holing 34.2(2003)154

Topic: Areas of shaded regions in a given configuration

Solution: Shades of Pythagoras 35.2(2004)139

749.

Proposer: Michael W. Ecker 34.2(2003)154

Topic: Existence of fully diversified sequences

Solution: To fully diversified and beyond 35.2(2004)140

750.

Proposer: Angelo S. DiDomenico 34.2(2003)154

Topic: Integer Solutions of an equation in 3 variables

Solution: A non-identity with many Solutions 35.2(2004)141

751.

Proposer: Seth Zimmerman 34.3(2003)239

Topic: Evaluation of sums involving the cardinality and products of integers in a set

Solution: A productive sum and its alternating counterpart 35.3(2004)228

752.

Proposer: Juan-Bosco Romero Márquez 34.3(2003)239

Topic: Exponential Diophantine equation in 2 variables

Solution: An asymmetric Diophantine equation 35.3(2004)229

753.

Proposer: Youngge Tian 34.3(2003)239

Topic: Identity involving the ranks of 2 idempotent matrices

Solution: A rank identity 35.3(2004)230

754.

Proposer: Andrew Cusumano 34.3(2003)240

Topic: Proving the existence of a positive sequence and finding its recurrence relation

Solution: A Stirling argument 35.3(2004)230

Proposer: Dean Hoffman & Peter Johnson 34.3(2003)240

Topic: Strategy needed to maximize the expected value in a gambling game

Solution: Strategy is unnecessary 35.3(2004)232

756.

Proposer: Michael Bataille 34.4(2003)327

Topic: Identity for the 6-term sum of ratios of sines Solution: A trigonometric identity 35.4(2004)312

757.

Proposer: W. V. Grounds 34.4(2003)327

Topic: Finding primes obtained from 2 different 4<sup>th</sup> degree polynomials in 2 variables

Solution: Two polynomials that rarely yield primes 35.4(2004)313

758.

Proposer: Gregory Dresden 34.4(2003)327

Topic: Differentiability and extreme values of a polar function

Solution: A critical parameter for a family of polar curves 35.4(2004)314

759.

Proposer: Götz Trenkler 34.4(2003)328

Topic: Necessary & sufficient condition that a matrix equation has a Solution

Solution: A matrix operation 35.4(2004)316

760.

Proposer: Arthur L. Holshouser 34.4(2003)328

Topic: Divisibility of and an inequality for a smallest value function

Solution: An inequality for an abstract function 35.4(2004)316

761.

Proposer: Charles L. Cooper & Michael Scott McClendon 34.5(2003)405

Topic: Circles and disks within disks

Solution: Disks in unions of discs 35.5(2004)403

762.

Proposer: Srinivasan Balaji & Hosam Mahmoud 34.5(2003)405

Topic: Characterizing a game matrix involving a tenable Pólya urn containing colored balls

Solution: Tenable Pólya urns 35.5(2004)404

763.

Proposer: Thomas J. Pfaff 34.5(2003)406

Topic: Find a function related to covering a circular cookie at depths in a vat of chocolate

Solution: Cookie rolling 35.5(2004)405

764.

Proposer: Kedar Hardikar 34.5(2003)406

Topic: Finding matrices of coordinates in n-dimensional vector spaces having determinant 0

Solution: Vandermonde variations 35.5(2004)406

Proposer: Angelo S. DiDomenico 34.5(2003)406

Topic: Find primitive quadruples of 4 positive integers satisfying a given condition

Solution: Radii in disguise 35.5(2004)407

766.

Proposer: Josè Luis Díaz-Barrero 35.1(2004)55

Topic: Inequality for coefficients of a polynomial with nonnegative roots

Solution: Roots and coefficients 36.1(2005)74

767.

Proposer: Ovidiu Furdui 35.1(2004)55

Topic: Series sum of e<sup>x</sup>- its Taylor partial sum Solution: Remainder in Taylor's formula 36.1(2005)75

768.

Proposer: Michel Bataille 35.1(2004)55

Topic: Hyperbolic identity depending on an exponential identity Solution: Hyperbolic and exponential functions 36.1(2005)76

769.

Proposer: Wenchang Chu & Leontina Veliana Di Claudio 35.1(2004)56

Topic: Binomial product identity

Solution: An expression for 2<sup>n</sup> 36.1(2005)77

770.

Proposer: Josè Luis Díaz-Barrero 35.1(2004)56 Topic: Logarithmic summation inequality Solution: A logarithmic inequality 36.1(2005)78

771.

Proposer: Yi-chuan Pan 35.2(2004)136

Topic: Infinitely many rational numbers guarantee 2 quadratics are squared rationals

Solution: An ancient and curious problem 36.2(2005)161

772.

Proposer: Yongge Tian 35.2(2004)136

Topic: Inequalities involving the ranks of 2 given idempotent matrices Solution: Rank inequalities for idempotent matrices 36.2(2005)162

773.

Proposer: Ovidiu Furdui 35.2(2004)136; Corrected 35.4(2004)310

Topic: Properties of cosines that involve lengths of a triangle

Solution: Powers of cosines and triangles 36.2(2005)163; Corrected 36.4(2005)332

774.

Proposer: Jody M. Lockhart 35.2(2004)136

Topic: Necessary & sufficient condition that the y-coordinate of points on a circle is zero

Solution: Points generated by geometric constructions 36.2(2005)163

Proposer: John H. Webb 35.2(2004)137

Topic: Inequalities involving a rational function of the sides of a triangle

Solution: An inequality in algebra and geometry 36.2(2005)164

776.

Proposer: Monte J. Zerger 35.3(2004)227

Topic: Find all idempotent pairs of matrices given 2 such matrices with idempotent products

Solution: Two-by-two idempotent pairs 36.3(2005)239

777.

Proposer: Michael Scott McClendon 35.3(2004)227

Topic: Is every interior point of every convex polygon m-trilinable? Solution: Non-convex polygons and m-trilinable points 36.3(2005)240

778.

Proposer: Will Gosnell 35.3(2004)227

Topic: Condition on 2 parameters that guarantee a given triple primitive Solution: A parametrization of the sides of right triangles 36.3(2005)241

779.

Proposer: Kedar Hardikar 35.3(2004)228

Topic: Evaluate an integral of an exponential vector function

Solution: An integral in linear algebra 36.3(2005)243

780.

Proposer: Josè Luis Díaz-Barrero 35.3(2004)228

Topic: Inequality involving a sum and an exponential function of Fibonacci numbers

Solution: An inequality involving Fibonacci numbers 36.3(2005)244

781.

Proposer: David Callan 35.4(2004)310

Topic: Probability involving wives, their girlfriends and husbands seated at a table

Solution: Sitting arrangements-wives and their girlfriends 36.4(2005)332

782.

Proposer: Talaat M. Abdin & Hosam M. Mahmoud 35.4(2004)310 Topic: Probability of a gambler in a losing position in a betting game

Solution: Losing a betting game 36.4(2005)333

783.

Proposer: Angelo S. DiDomenico 35.4(2004)311

Topic: Triangles with equal area triangles with and a necessary & sufficient condition for

equal products of sides

Solution: Constructions and concurrency 36.4(2005)335

784.

Proposer: Kent Holing 35.4(2004)311

Topic: Lengths that cannot be sides of a right triangle and some that cannot form a square

Solution: Pythagorean triples, Pythagorean triangles, and squares 36.4(2005)337

Proposer: Josè Luis Díaz-Barrero 35.4(2004)311

Topic: Inequality involving sides, cosines and the inradius of a triangle Solution: A trigonometric inequality involving in-radius 36.4(2005)338

786.

Proposer: Michael Golomb 35.5(2004)402

Topic: Find conjugate diameters of an ellipse intersecting an arc of maximum length

Solution: Conjugate diameters of an ellipse 36.5(2005)414

.787.

Proposer: Michel Bataille 35.5(2004)402; Corrected 36.1(2005)73 Topic: Find the roots of a recursively defined polynomial equation Solution: Roots of recursively defined polynomials 36.5(2005)415

788.

Proposer: Elias Lampakis 35.5(2004)402

Topic: Find bounds for the probability that a hyperbola has no integer points Solution: The odds of having integer points on a hyperbola 36.5(2005)415

789.

Proposer: Zengxiang Tong & Zhen Huang 35.5(2004)403

Topic: Show convergence and find limits of 2 sequences related to nested roots of 2

Solution: Sequences converging to  $\pi$  36.5(2005)416

790.

Proposer: Elliott Cohen 35.5(2004)403

Topic: Properties of the rank of a family of determinants of columns of a complex matrix

Solution: Ranks: matrices and linear forms 36.5(2005)418

791.

Proposer: Gregory Fredricks & Roger Nelson 36.1(2005)73

Topic Row and column sums of a (must be) square matrix 36.1(2005)73

Solution: Sufficient conditions for square matrices 37.1(2006)62

792.

Proposer: Josè Luis Díaz-Barrero 36.1(2005)73

Topic: Sum-Product inequality of a positive sequence 36.1(2005)73

Solution: A particular case of an inequality 37.1(2006)63

793.

Proposer: William P. Wardlaw 36.1(2005)74

Topic: Symmetric groups and inner automorphisms 36.1(2005)74

Solution: The making of an inner automorphism for  $A_n$  37.1(2006)64

794.

Proposer: W. C. Gosnell 36.1(2005)74

Topic: Circle with an angle subtended by an arc of a certain length 36.1(2005)74

Solution: Existence of some special central angles 37.1(2006)65

Proposer: Göt Trenkler 36.1(2005)74

Topic: Trace identities of a complex matrix 36.1(2005)73

Solution: Necessary & sufficient condition for  $A^2 = -A$  37.1(2006)67

796.

Proposer: Andrew Cusumano 36.2(2005)160; Corrected: 36.4(2005)330; 37.2(2006)144

Topic: Convergence of 2 series of reciprocals of products of Fibonacci numbers

Solution: Infinite sums defined by the Fibonacci sequence 37.4(2006)309

797.

Proposer: Josè Luis Díaz-Barrero 36.2(2005)161

Topic: Inequalities involving finite sums of squares of secant functions Solution: Endpoint-approximation of a definite integral 37.2(2006)145

798.

Proposer: Willaim P. Wardlaw 36.2(2005)161

Topic: What characteristic polynomials completely determine the rank of a matrix?

Solution: Rank of A and det (xI - A) 37.2(2006)146

799.

Proposer: Mohammad K. Azarian 36.2(2005)161

Topic: Limit of a series involving terms of a 2<sup>nd</sup> order recurrence relation

Solution: A limit expression of 1/(e - 1) 37.2(2006)147

800.

Proposer: Hojoo Lee 36.2(2005)161

Topic: Show a cubic polynomial satisfying given inequalities is positive for positive values

Solution: Conditions for non-negative cubic polynomials 37.2(2006)148

801.

Proposer: Nora Thornber 36.3(2005)238

Topic: First order matrix differential equation

Solution: Generalization of an old CMJ problem 37.3(2006)230

802.

Proposer: Willaim P. Wardlaw 36.3(2005)239

Topic: Probability that the product of 2 randomly chosen matrices is the identity matrix

Solution: The probability that AB = I 37.3(2006)232

803.

Proposer: Yongge Tian 36.3(2005)239

Topic: Show a matrix of given matrices is an orthogonal projector and construct another Solution: An orthogonal projector consisting of non-negative matrices 37.3(2006)233 804.

Proposer: Mohammad Riazi-Kermani & Hongbiao Zeng 36.3(2005)239

Topic: Find a sufficient condition that an nth degree polynomial has a complex root Solution: Polynomials: A sufficient condition for a non-real zero 37.3(2006)234

Proposer: Josè Luis Díaz-Barrero 36.3(2005)239 Topic: Inequality involving Fibonacci numbers

Solution: An inequality involving the fourth power of Fibonacci numbers 37.3(2006)235

806.

Proposer: Kenneth Fogarty 36.4(2005)331

Topic: Lengths of sequences of derived triangles from a given triangle

Solution: A sequence of triangles 37.4(2006)311

807.

Proposer: Angelo S. DiDomenico 36.4(2005)331

Topic: Necessary & sufficient condition on 4 integers generating all Pythagorean triples

Solution: Conditions for primitive Pythagorean triples 37.4(2006)312

808.

Proposer: Yongge Tian 36.4(2005)331

Topic: Equality of ranks of matrices related to a given positive definite matrix

Solution: An equality for ranks of symmetric positive definite matrices 37.4(2006)313 809.

Proposer: Ovidui Furdui 36.4(2005)331

Topic: Limit of a sum involving roots of integers

Solution: A limit expression of  $(\ln 2)^2$  37.4(2006)314

810.

Proposer: Josè Luis Díaz-Barrero 36.4(2005)331

Topic: Limit of a sum of square roots of a ratio of polynomials in 2 variables

Solution: A limit computed by integration 37.4(2006)316

811.

Proposer: Willaim Wardlaw 36.5(2005)413

Topic: Find the characteristic polynomial of the adjoint of a matrix with a 5<sup>th</sup> degree one

Solution: Characteristic polynomial of the adjoint of a matrix 37.5(2006)393

812.

Proposer: Ovidui Furdui 36.5(2005)413; Corrected: 37.2(2006)143

Topic: Find the limit of the difference of exponential functions of sums of sines

Solution: A limit related to Euler's constant 38.2(2007)150

813.

Proposer: Mohammad K. Azarian 36.5(2005)413

Topic: Establishing the sum of perpendicular lengths formed in 45 nested triangles

Solution: Forty-five nested equilateral triangles and csc 1° 37.5(2006)394

814.

Proposer: Josè Luis Díaz-Barrero 36.5(2005)414

Topic: Find the minimum value of a sum of ratios of 3 positive numbers Solution: Minimizing a constrained symmetric expression 37.5(2006)396

Proposer: Youngge Tian 36.5(2005)414

Topic: Necessary & sufficient condition for the ranges of Kronecker products of matrices

Solution: Comparing ranges of Kronecker products of matrices 37.5(2006)397

816.

Proposer: Ovidui Furdui 37.1(2006)59

Topic: Find the minimum number that allows 3 given sine terms to be the sides of a triangle

Solution: Building triangles for a triangle 38.1(2007)61

817.

Proposer: Mohammad K. Azarian 37.1(2006)59

Topic: Find values allowing a given slope to the graph of a function with given derivative

Solution: Slopes of tangents 38.1(2007)63

818.

Proposer: Angelo S. DiDomenico 37.1(2006)60

Topic: Identity for 5 consecutive elements in a recurrence relation

Solution: A Fibonacci-like sequence 38.1(2007)64

819.

Proposer: Michael Andreoli 37.1(2006)60

Topic: Evaluate the sum of recipocals of products of consecutive integers

Solution: An interesting and well known series 38.1(2007)65

820.

Proposer: Greg Oman 37.1(2006)60

Topic: Necessary condition that a commutative ring with identity has non associates

Solution: Non-associates 38.1(2007)66

821.

Proposer: Andrew Cusumano 37.2(2006)143

Topic: Limit of the difference of ratios of sums of powers of integers

Solution: An expression of e 38.2(2007)150

822.

Proposer: Götz Trenkler 37.2(2006)143

Topic: Show that a given matrix and its conjugate transpose have the same column space Solution: Column space of a square matrix and its conjugate transpose 38.2(2007)152

823.

Proposer: Michel Bataille 37.2(2006)144

Topic: Inequality for the product of powers of tangents and sines

Solution: A trigonometric inequality 38.2(2007)153

824.

Proposer: Jeremy Leach 37.2(2006)144

Topic: Evaluate a double sum involving binomial coefficients and factorials

Solution: Always 2 38.2(2007)154

Proposer: Juan-Bosco Romero Márquez 37.2(2006)144 Topic: Find the limit of the ratio of 2 improper integrals

Solution: Two improper integrals and L'Hospital's rule 38.2(2007)155

826.

Proposer: Parviz Khalili 37.3(2006)229

Topic: Evaluate an improper integral of a reciprocal of sums of 4<sup>th</sup> powers

Solution: Evaluation of an improper integral 38.3(2007)228

827.

Proposer: Syrous Marivani 37.3(2006)229

Topic: Evaluate sums of Fibonacci numbers and sums of Lucas numbers Solution: Sums related to Fibonacci and Lucas sequences 38.3(2007)230

828.

Proposer: Michael McClendon 37.3(2006)230

Topic: Find parametric equations of a curve with given intercepts to tangent lines

Solution: The cycloid 38.3(2007)231

829.

Proposer: Dimitri Thoro & Linda Valdes 37.3(2006)230

Topic: Finding distances between 2 parallelopipeds cut by a plane

Solution: Cutting a rectangular parallelopiped 38.3(2007)232

830.

Proposer: Roger Bilisoly 37.3(2006)230; Corrected: 37.4(2006)308; 37.5(2006)392 Topic: Finding the area of an alternating n-gon with sides satisfying given conditions

Solution: Area of an alternating 2n-gon 38.5(2007)389

831.

Proposer: Stanley Rabinowitz 37.4(2006)308

Topic: Identities involving tangents and sines of specific angles

Solution: The tangent function and  $\sqrt{11}$  38.4(2007)310

832.

Proposer: Ken Holing 37.4(2006)309

Topic: Necessary & sufficient condition that the Galois group of a quartic polynomial

equation is cyclic

Solution: Conditions for a cyclic Galois group of a quadratic equation 38.4(2007)312

833.

Proposer: Angelo S. DiDomenico 37.4(2006)309

Topic: Finding Heronian triangles with conditions on their sides and perimeter

Solution: Generating Heronian triangles 38.4(2007)315

834.

Proposer: Josè Luis Díaz-Barrero 37.4(2006)309

Topic: Inequality involving cube roots of ratios of Fibonacci numbers

Solution: An inequality with Fibonacci numbers and cube roots 38.4(2007)316

Proposer: Juan-Bosco Romero Márquez 37.4(2006)309

Topic: Inequalities involving cubes of sums of 3 positive numbers

Solution: An inequality involving cubes 38.4(2007)317

836.

Proposer: Josè Luis Díaz-Barrero 37.5(2006)392

Topic: Inequality involving sums and powers of 3 real numbers Solution: An inequality with cyclosymmetric functions 38.5(2007)390

837.

Proposer: Juan-Bosco Romero Márquez 37.5(2006)392

Topic: Inequalities involving the sides and inradius of a triangle

Solution: Inequalities from the inscribed circle of a triangle 38.5(2007)391

838.

Proposer: Arkady Alt 37.5(2006)393

Topic: Inequality for reciprocals of sums and differences of squared sides of a triangle

Solution: An acute triangle inequality 38.5(2007)392

839.

Proposer: Andrew Cusumano 37.5(2006)393

Topic: Find the general term and limit of a sequence of sums of reciprocals of integers

Solution: The general term and limit of a sequence 38.5(2007)393

840.

Proposer: Ruthven Murgatroyd 37.5(2006)393

Topic: Moving circular segments around a right angled hallway

Solution: Area of a circle segment and length of its chord 38.5(2007)395

841.

Proposer: Mohammad K. Azarian 38.1(2007)60

Topic: Find value of 2 fixed points of a quadratic polynomial Solution: Fixed points of a quadratic polynomial 39.1(2008)66

842.

Proposer: Hongbiao Zeng 38.1(2007)60

Topic: Show existence of a point on the surface of a cube satisfying a distance condition

Solution: An inequality of a k-dimensional unit cube 39.1(2008)67

843.

Proposer: P. R. Parthasarathy 38.1(2007)60

Topic: Equality of n summations of powers of a number in (0,1) to a given determinant

Solution: An expression of a determinant 39.1(2008)68

844.

Proposer: Ovidui Furdui 38.1(2007)61

Topic: Identity for the sum of a sequence involving Euler's constant

Solution: Infinite series and Euler's constant 39.1(2008)71

Proposer: Mohsen Soltanifar 38.1(2007)61

Topic: Continuity of a given Riemann-integrable function which is an integral's derivative

Solution: Derivatives of integrals 39.1(2008)6672

846.

Proposer: Josè Luis Díaz-Barrero

Topic: Inequality involving sums of reciprocals of powers of binomial coefficients

Solution: An inequality with the sum of combinations 39.2(2008)154

847.

Proposer: Juan-Bosco Romero Márquez

Topic: Inequalities for the inradius, circumradius and semi-perimeter of a triangle

Solution: Inequalities with inradius and circumradius 39.2(2008)155

848.

Proposer: Angelo S. DiDomenico 38.2(2007)149

Topic: Identities for generalized Fibonacci-like sequences

Solution: An identity for Fibonacci-like sequences 39.2(2008)157

849.

Proposer: Gregory L. Wilson 38.2(2007)149

Topic: Probability concerning life spans of contemporaries Solution: Probability for two contemporaries 39.2(2008)158

850.

Proposer: Charles Redmond 38.2(2007)149

Topic: Properties of eigenvectors for a given matrix

Solution: Positive eigenvalues 39.2(2008)159

851.

Proposer: Josè Luis Díaz-Barrero 38.3(2007)227

Topic: Finding eigenvalues of the sum of 2 projection matrices

Solution: A conditional inequality 39.3(2008)241

852.

Proposer: Frank Morgan 38.3(2007)227; Clarification: 39.1(2008)65

Topic: Finding eigenvalues of two orthogonal projection matrices 38.3(2007)227 Solution Eigenvalues of the sum of two orthogonal projection matrices 40.1(2009)56 853.

Proposer: Angelo S. DiDomenico 38.3(2007)227

Topic: Padoa's inequality and locating a point on a triangle whose sides satisfy it

Solution: A generalization of Padoa's inequality 39.3(2008)242

854.

Proposer: Ovidui Furdui 38.3(2007)228

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Proposer: Michel Bataille 38.3(2007)228

Topic: Identity involving products of sums of functions of floor function

Solution: A floor function equality 39.3(2008)245

856.

Proposer: Victor Dontsov, Evgeni Maevski & Zokhrab Mustafaev 38.4(2007)309

Topic: Limit of a sum of n<sup>th</sup> roots of consecutive integers Solution: A sequence whose limit is 2007! 39.4(2008)308

857.

Proposer: Claud Bégin 38.4(2007)309

Topic: Finding points which yield a given number of tangents to the graph of a cubic Solution: The number of tangents to the graph of a cubic function 39.4(2008)309

858.

Proposer: Ayoub B. Ayoub 38.4(2007)309

Topic: Properties of triangles constructed on the sides of a quadrilateral

Solution: 90° rotations of triangles about a point 39.4(2008)311

859.

Proposer: Josè Luis Díaz-Barrero 38.4(2007)310

Topic: Limit of a sum of integrals involving the logarithmic function Solution: Limit of the sum of some improper integrals 39.4(2008)312

860.

Proposer: David Finn & Herb Bailey 38.4(2007)310

Topic: Property of a hexagon constructed from extending the sides of a triangle

Solution: Conditions for cyclic hexagon 39.4(2008)313

861.

Proposer: Angelo S. DiDomenico 38.5(2007)388

Topic: Existence of integers, a, b, and c, whose sum is a perfect number, and such that

(a + b, a + c, b + c) is a Pythagorean triple

Solution: Even perfect numbers and Pythagorean triples 39.5(2008)403

862.

Proposer: Elias Lampakis 38.5(2007)388

Topic: Existence of 27 rational coefficients which can generate a sequence from itself

Solution: A splitting field over the rationals 39.5(2008)404

863.

Proposer: Mohsen Soltanifar 38.5(2007)388

Topic: Existence of continuumly many metrics for which a given sequence converges

Solution: Continuumly many matrices 39.5(2008)406

864.

Proposer: Dennis Walsh 38.5(2007)389

Topic: Double sum of a sequence depending on 2 indices

Solution: An expression for e 39.5(2008)407

Proposer: Spiros P. Andriopoulos 38.5(2007)389

Topic: Inequality for a double integral of logarithmic functions over polar region

Solution: A lower bound for a double integral 39.5(2008)408

866.

Proposer: Edwin F. Sampang 39.1(2008)65

Topic: Evaluation of a given fraction from two given fractions Solution: Evaluating a fraction of the form z/(y + z) 40.1(2009)58

867.

Proposer: Josè Luis Díaz-Barrero 39.1(2008)66

Topic: Inequality involving the arithmetic and geometric mean of 4 numbers Solution: A consequence of the arithmetic-geometric inequality 40.1(2009)59

868.

Proposer: A. R. Miller 39.1(2008)66

Topic: Evaluation of a sum of the reciprocal product of gamma functions

Solution: A double sum with the gamma function 40.1(2009)60

869.

Proposer: Vicențiu Rădulescu 39.1(2008)66

Topic: Product of a function and its 2<sup>nd</sup> derivative inequality

Solution: No such function 40.1(2009)61

870.

Proposer: Mohammad K. Azarian 39.1(2008)66 Topic Evaluating a sum of definite integrals Solution: An expression for  $\pi$  40.1(2009)62

871.

Proposer: Greg Oman 39.2(2008)153

Topic: Find positive integers so a given equation in 2 variables has integral Solutions

Solution: Pythagorean-triple Solutions 40.2(2009)132

872.

Proposer: Josè Luis Díaz-Barrero 39.2(2008)153

Topic: Inequality for a finite sum of powers of reciprocals of factorials

Solution: A lower bound for  $1/(n!)^2$  40.2(2009)133

873.

Proposer: Ovidui Furdui 39.2(2008)154

Topic: Evaluate infinite series of logarithm terms

Solution: Stieltjes constants 40.2(2009)136

874.

Proposer: Michael S. Becker 39.2(2008)154

Topic: Show that a sum of even derivatives divided by factorials is 1

Solution: An infinite sum with  $f^{(4n)}(1)$  and  $f^{(2n)}(1)$  40.2(2009)137

Proposer: Dorin Marghidanu 39.2(2008)154

Topic: Inequalities involving square roots of products of 4 positive numbers

Solution: Two cycle inequalities 40.2(2009)139

876.

Proposer: Jody M. Lockhart & William P. Wardlaw 39.3(2008)240

Topic: Mod numbers for which rings of polynomials are groups of units

Solution: When does  $Z[x]^* = Z^*_m$ ? 40.3(2009)216

877.

Proposer: Ovidui Furdui 39.3(2008)241

Topic: Sequence of improper integrals to be evaluated

Solution: The answer is n! ln 2 40.3(2009)217

878.

Proposer: Josè Luis Díaz-Barrero 39.3(2008)241

Topic: Inequality involving the sides and semi-perimeter of a triangle

Solution: A cyclical inequality for a triangle 40.3(2009)218

879.

Proposer: Dorin Marghidanu 39.3(2008)241

Topic: Inequalities for the coefficients of a 4<sup>th</sup> degree polynomial Solution: Roots and coefficients of a quadratic function 40.3(2009)219

880.

Proposer: Bianca-Teodora Iordache 39.3(2008)241

Topic: An Inequality for a sum of powers of terms of a sequence and a necessary &

sufficient condition that equality holds

Solution: An application of some inequalities 40.3(2009)220

881.

Proposer: Kim McInturff 39.4(2008)307

Topic: Identity for a finite sum of binomial coefficients and a sum of sine terms

Solution: Representations of a generating function 40.4(2009)294

882.

Proposer: Oskar Maria Baksalary 39.4(2008)307 Topic: Inequality involving vectors and matrices

Solution: An inequality with positive definite matrices 40.4(2009)296

883.

Proposer: Brian Bradie 39.4(2008)308

Topic: Evaluate 2 integrals, one involving an arctangent, and the other a logarithm

Solution: Two closely related definite integrals 40.4(2009)297

884.

Proposer: Josè Luis Díaz-Barrero 39.4(2008)308

Topic: Evaluate the limit of a double sum involving products of integers

Solution: The limit of a double sum 40.4(2009)299

Proposer: Ovidui Furdui 39.4(2008)308

Topic: Evaluate an improper double integral involving the square of a logarithm

Solution: A double integral and the Dirichlet beta function 40.4(2009)300

886.

Proposer: Árpád Bényi 39.5(2008)401

Topic: Properties of a "good" function composed with itself 2008 times

Solution: A good function 40.5(2009)377

887.

Proposer: Josè Luis Díaz-Barrero 39.5(2008)402

Topic: Evaluate a finite sum of ratios of roots of unity and their conjugates

Solution: A sum involving odd roots of unity 40.5(2009)378

888.

Proposer: Brian Bradie 39.5(2008)402

Topic: Find the limit of a product of powers of a binomial Solution: The limit of a Riemann sum 40.5(2009)380

889.

Proposer: Jody M. Lockhart & William P. Wardlaw 39.5(2008)402 Topic: Find how many  $4\times4$  matrices have a given determinant Solution: The number of  $4\times4$  matrices over  $F_8$  40.5(2009)382

890.

Proposer: Russell Hendel 39.5(2008)402

Topic: Proving that a given n<sup>th</sup> order recurrence relation may or may not exist

Solution: Another family of recursions 40.5(2009)382

891.

Proposer: William P. Wardlaw 40.1(2009)55

Topic: Determining an ordered basis for a certain vector space

Solution: An ordered basis for an *n*-dimensional space over a field 41.1(2010)65

892.

Proposer: Greg Oman 40.1(2009)55

Topic: Finding all rings with certain given properties Solution: A characterization of a finite field 41.1(2010)66

893.

Proposer: Ovidui Furdui 40.1(2009)56

Topic: Summing products of x<sup>n</sup> and the difference of a function and its Taylor polynomial

Solution: An infinite sum of a function with its Taylor polynomial 41.1(2010)67

894.

Proposer: Juan-Bosco Romero Márquez 40.1(2009)56

Topic: Inequality involving the in- and circum- radii of a triangle

Solution: Two triangle inequalities 41.1(2010)69

Proposer: Ovidui Furdui 40.1(2009)56

Topic: Evaluation of a product of powers of a ratio of integers

Solution: The limit of an infinite product 41.1(2010)70

896.

Proposer: Darij Grinberg 40.2(2009)131 Topic: Algebraic inequality in 3 variables

Solution: A constrained homogeneous inequality 41.2(2010)161

897.

Proposer: R. S. Tiberio 40.2(2009)131

Topic: Perpendicular segments from a triangle's circumcenter to its centroid and to its

Nagel point

Solution: Nagel point, Euler line, and Fuhrmann circle 41.2(2010)161

898.

Proposer: Mihály Bencze 40.2(2009)131

Topic: Inequality for definite integrals of a function with nonnegative 2<sup>nd</sup> derivative Solution: An inequality with definite integrals of a convex function 41.2(2010)166

899.

Proposer: Ovidui Furdui 40.2(2009)132

Topic: Limit of a definite integral of a ratio of polynomials

Solution: A definite integral involving a geometric series 41.2(2010)167

900.

Proposer: Michel Bataille 40.2(2009)132

Topic: Summation equality involving the finite harmonic series and its square

Solution: An identity with the harmonic series 41.2(2010)169

901.

Proposer: Cezar Lupu 40.3(2009)215

Topic: Square root inequality in 3 positive numbers

Solution: A cyclic inequality 41.3(2010)243

902.

Proposer: Mohsen Soltanifar 40.3(2009)215; Clarified: 41.3(2010)242

Topic: Convergence of a sum of ratios of powers of a sequence Solution: Conditions of convergence of a series 42.3(2011)233

903.

Proposer: José Luis Díaz-Barrero and José Gibergans-Báguena 40.3(2009)216

Topic: Inequality involving squares of sums of ratios of square roots Solution: An inequality with telescoping summation 41.3(2010)244

904.

Proposer: Ovidiu Furdui 40.3(2009)216

Topic: Double integral of the log of the gamma function of 2 variables Solution: A double integral with the Gamma function 41.3(2010)245

Proposer: Ovidiu Furdui 40.3(2009)216

Topic: Integral involving the fractional part of a number

Solution: The Euler-Mascheroni constant in the form of an integral 41.3(2010)246

906.

Proposer: Ovidiu Furdui 40.4(2009)293

Topic: Infinite product of a product of fractions

Solution: The Gamma function and an infinite product 41.4(2010)330

907.

Proposer: Brian Bradie 40.4(2009)293

Topic: Sum involving Pell-Lucas numbers

Solution: An infinite sum with the Pell-Lucas numbers 41.4(2010)332

908.

Proposer: Scott Duke 40.4(2009)294

Topic: Sequence whose convergence depends on the Riemann zeta function

Solution: Limit of a recursive sequence 41.4(2010)333

909.

Proposer: Francisco Javier Garcia 40.4(2009)294

Topic: Show that a quadrilateral constructed from the incenter of a triangle is cyclic

Solution: Reflection and cyclic quadrilateral 41.4(2010)333

910.

Proposer: Michael Goldenberg & Mark Kaplan 40.4(2009)294

Topic: Show that a ratio of determinants of Tribonacci numbers is a perfect square

Solution: determinants based on a tribonacci sequence 41.4(2010)335

911.

Proposer: Michael Scott McClendon 40.5(2009)376

Topic: Determining if a 7-gon is externally trilinable

Solution: An externally trilinable 7-gon 41.5(2010)410

912.

Proposer: Kenneth W. Fogarty 40.5(2009)376

Topic: Evaluating a product of quadratics defined on a given sequence

Solution: Product of function images and recursion 41.5(2010)411

913.

Proposer: Mihály Bencze 40.5(2009)376

Topic: Inequality involving sums and products of a given sequence Solution: An inequality with a finite sum of products 41.5(2010)412

914.

Proposer: Y. N. Aliyev 40.5(2009)377

Topic: Finding numbers in square roots whose fractional parts satisfy a given condition

Solution: The fractional part of a real number 41.5(2010)413

Proposer: Will Gosnell & Herb Bailey 40.5(2009)377

Topic: Expressing the hypotenuse of a certain right triangle in terms of the gold ratio

Solution: A right triangle and the golden ratio 41.5(2010)414

916.

Proposer: Kim McInturff 41.1(2010)64

Topic: An integral involving the gamma function

Solution: A definite integral and the Glaisher-Kinkelin constant 42.1(2011)63

917.

Proposer: José Luis Díaz-Barrero 41.1(2010)64

Topic: Inequalities involving the sides, inradius and the circumradius of a triangle Solution: An inequality of a triangle with its circumradius and inradius 42.1(2011)66

918.

Proposer: Cezar Lupu 41.1(2010)64

Topic: When is an expression involving three integers a perfect cube?

Solution: Conditions for a perfect cube 42.1(2011)67

919.

Proposer: Michel Bataille 41.1(2010)65

Topic: Identities involving the sides, inradius and the radii of the excircles of a triangle

Solution: Two triangle identities 42.1(2011)68

920.

Proposer: Ovidiu Furdui 41.1(2010)65

Topic: Absolute convergence of a series involving products of cosines

Solution: An infinite sum with the power of a product of cosines 42.1(2011)69

921.

Proposer: Ovidiu Furdui 41.2(2010)160

Topic: Inequalities involving sequences of towers

Solution: Bounes for two subsequences of {1/k [towered by 1/k, k times]} 42.2(2011)152

922.

Proposer: Sadi Abu-Saymeh & Mowaffag Hajja 41.2(2010)161

Topic: Equality of distances arising from angle bisectors of angles of a triangle

Solution: An isosceles triangle problem again 42.2(2011)155

923.

Proposer: Eugen J. Ionascu 41.2(2010)161

Topic: Construct a sequence of numbers and determine the limit of the mean of their sums

Solution: Constructing a sequence satisfying certain properties 42.2(2011)156

924.

Proposer: Joe Howard 41.2(2010)161

Topic: Inequality involving a finite sequence whose terms have a product equal to unity

Solution: A result from the AM-GM inequality 42.2(2011)157

Proposer: Cezar Lupu & Tudorel Lupu 41.2(2010)161

Topic: Existence of a vanishing point of the 2<sup>nd</sup> derivative of a function satisfying integrals

Solution: Conditions for f'' = 0 with  $c \in (0,1)$  42.2(2011)158

926.

Proposer: Mowaffaq Hajja 41.3(2010)242

Topic: Constructing cevians which make equal angles with the base of a triangle

Solution: Equal cevian intercepts 42.3(2011)235

927.

Proposer: Cezar Lupu & Tudorel Lupu 41.3(2010)242

Topic: Inequality involving the difference of two integrals of a differentiable function Solution: An inequality of a function with continuous first derivative 42.3(2011)236

928.

Proposer: Michel Bataille 41.3(2010)243

Topic: Necessary and sufficient conditions that the rank of two special matrices are equal

Solution: Conditions for Rank(A) = Rank(B0 42.3(2011)237

929.

Proposer: Cezar Lupu & Vlad Matei 41.3(2010)243

Topic: Inequality involving the sum of the cubes of three real numbers

Solution: A constrained inegiality 42.3(2011)238

930.

Proposer: Ovidui Furdui 41.3(2010)243

Topic: Evaluating the integral of a function with a given finite limit as x approaches infinity

Solution: An application of the Weierstrass Approximation Theorem 42.3(2011)239

931.

Proposer: Sam Vandervelde 41.4(2010)329

Topic: Equality involving two polynomials and the form of the remainder of their ratio

Solution: Composition and product of polynomials 42.4(2011)330

932.

Proposer: Cezar Lupu & Tudorel Lupu 41.4(2010)329

Topic: Integral inequality involving the 4<sup>th</sup> power of a continuous function on [0,1]

Solution: A simple inequality for a definite integral 42.4(2011)332

933.

Proposer: Cosmin Pohoată 41.4(2010)329

Topic: Inequality involving the inradii of triangles formed from the orthocenter of a triangle

Solution: An inequality with inradii 42.4(2011)332

934.

Proposer: José Luis Díaz-Barrero 41.4(2010)330

Topic: Summation inequality involving the sides and semi-perimeter of an n-gon

Solution: An inequality of n-gons 42.4(2011)334

Proposer: Tom Beatty 41.4(2010)330

Topic: Two person game where players alternately select irrational numbers and integers

Solution: Winning strategy 42.4(2011)335

936.

Proposer: Cezar Lupu & Tudorel Lupu 41.5(2010)409 Topic: Inequality involving 3 positive real numbers

Solution: A symmetric inequality in three variables 42.5(2011)408

937.

Proposer: Panagiote Ligouras 41.5(2010)409

Topic: Inequality involving medians, angle bisectors and the circumradius of a triangle

Solution: Inequality from a triangle 42.5(2011)409

938.

Proposer: Ovidiu Furdui 41.5(2010)409

Topic: Integral limit of involving integers *n* and polynomials times an integrable function

Solution: The limit related to a definite integral 42.5(2011)410

939.

Proposer: Cezar Lupu 41.5(2010)410

Topic: Necessary and sufficient conditions that the trace of the adjugate of a matrix is zero

Solution: An adjugate problem 42.5(2011)411

940.

Proposer: Greg Oman 41.5(2010)410

Topic: Find rings that require the product of members of a sequence be in the sequence

Solution: Identification of some nonzero rings 42.5(2011)412

941.

Proposer: Ovidiu Furdui 42.1(2011)62

Topic: Evaluating the limit of an integral of a product of two functions

Solution: Evaluating and integral limit 43.1(2012)96

942.

Proposer: Geoffrey Kandall 42.1(2011)62

Topic: Sum of ratios involving angle bisectors intersecting at the incenter of a triangle

Solution: An equation in geometry 43.1(2012)98

943.

Proposer: Juan-Bosco Romero Márquez & Francisco Javier García Capitán 42.1(2011)62 Topic: Locating points on an internal bisector in a triangle which satisfy a given cross ratio

Solution: A cross ratio problem 43.1(2012)99

944.

Proposer: Duong Viet Thong 42.1(2011)63

Topic: Inequalities involving the integral of a continuously differentiable function

Solution: The bounds of a definite integral 43.1(2012)100

Proposer: Erwin Just 42.1(2011)63

Topic: Existence of an integer in a ring which satisfies a given equation and 3 conditions

Solution: Properties of some rings 43.1(2012)103

946.

Proposer: Greg Oman 42.2(2011)151

Topic: For a function, f, defined on a countable set find a sequence satisfying  $f(x_n) x_{n+1}$ 

Solution: Ordering a countably infinite set with a function 43.2(2012)175

947.

Proposer: Ovidiu Furdui 42.2(2011)151

Topic: Finding all polynomials, P and Q such that for i = 1,...,n,  $\prod P(i) = Q(\prod i)$ 

Solution: Identifying some polynomials 43.2(2012)176

948.

Proposer: Duong Viet Thong 42.2(2011)151

Topic: Inequality involving the integral of a continuously differentiable function

Solution: An integral inequality 43.2(2012)177

949.

Proposer: Cezar Lupu 42.2(2011)152

Topic: Identities involving integrals of continuously differentiable functions

Solution: Forming integral equations 43.2(2012)178

950.

Proposer: José Luis Díaz-Barrero 42.2(2011)152

Topic: Inequality involving ratios three numbers summed over all their cyclic permutations

Solution: A constrained inequality 43.2(2012)179

951.

Proposer: Duong Viet Thong 42.3(2011)232

Topic: Existence of a number relating to the derivative of a function satisfying 3 integrals

Solution: Mean value theorem for integral 43.3(2012)258

952.

Proposer: Michel Bataille 42.3(2011)232

Topic: Summing a product of binomial coefficients and powers of two

Solution: A binomial coefficient identity 43.3(2012)260

953.

Proposer: Tom Beatty 42.3(2011)232

Topic: Summing a sequence of numbers satisfying a given non-linear recurrence

Solution: A recursively defined series 43.3(2012)261

954.

Proposer: Edwin Just 42.3(2011)233

Topic: Determining two counterfeit coins in a set of twelve

Solution: Detecting two fake coins 43.3(2012)262

Proposer: José Luis Díaz-Barrero 42.3(2011)233

Topic: Inequality involving ratios three numbers summed over all their cyclic permutations

Solution: Another constrained inequality 43.3(2012)263

956.

Proposer: Duong Viet Thong 42.4(2011)329

Topic: Existence of 3 numbers related to a function whose definite integral is 1 Solution: Guaranteeing three function values whose products is 1 43.4(2012)338

957.

Proposer: Michel Bataille 42.4(2011)329

Topic: Divisibility and a summation involving Fibonacci numbers

Solution: Properties of Fibonacci numbers 43.4(2012)339

958.

Proposer: Mohammad Azarian 42.4(2011)330

Topic: Summation involving a sequence defined by a 2<sup>nd</sup> order nonlinear recurrence relation

Solution: Sylvester's sequence and the infinite Egyptian fraction decomposition of 1

43.4(2012)340

959.

Proposer: Michael Goldberg & Mark Kaplan 42.4(2011)330

Topic: Identity involving a sequence defined by a 3<sup>rd</sup> order recurrence relation

Solution: An identity for a Fibonacci-like sequence 43.4(2012)342

960.

Proposer: Peter Ash 42.4(2011)330

Topic: Identity of products of square roots involving three positive numbers

Solution: de Gua's theorem 43.4(2012)343

961.

Proposer: Andrew Simoson 42.5(2011)407

Topic: Proving the difference of two inverse sine functions is a constant

Solution: A constant function with arcsin 43.5(2012)411

962.

Proposer: Juan-Bosco Romero Màrquez 42.5(2011)407

Topic: Inequalities involving the inradius and circumradius of a triangle

Solution: Inequalities of a non-acute angle 43.5(2012)413

963.

Proposer: Duong Viet Thong 42.5(2011)407 Topic: Inequality involving definite integrals Solution: An integral inequality 43.5(2012)414

964.

Proposer: Jerry Minkus 42.5(2011)408

Topic: Identities involving the angles and internal points of a triangle

Solution: Equalities with incenter, circumcenter, and orthocenter 43.5(2012)416

Proposer: James Duemmel 42.5(2011)408

Topic: Properties of a sequence formed from a well-known inequality

Solution: Properties of a sequence 43.5(2012)417

966

Proposer: Tahani Fraiwan & Mowaffaq Hajja 43.1(2012)95

Topic: Necessary and sufficient conditions relating to the cevians of a triangle

Solution: Cevians, midpoint and equal areas 44.1(2013)66

967

Proposer: Elias Lampakis 43.1(2012)95

Topic: Prove the tangent lines to a parabola and a polynomial intersect in irrational points

Solution: Irrational intersecting points 44.1(2013)67

968

Proposer: Greg Oman 43.1(2012)95

Topic: Prove or disprove that all members of a ring of monotone functions are constant

Solution: Rings of monotonic functions 44.1(2013)68

969

Proposer: Panagiote Ligouras 43.1(2012)96

Topic: Inequality relating to the sides of a given hexagon

Solution: Hexagon inequality 44.1(2013)69

970

Proposer: Xiang-Qian Chang 43.1(2012)96

Topic: Inequality relating to the traces of a symmetric matrix

Solution: Matrix inequalities 44.1(2013)70

971

Proposer: George Apostolopoulos 43.2(2012)174

Topic: Summation inequality involving 3 variables and their permutations

Solution: An application of the AM-GM inequality 44.2(2013)143

972

Proposer: Elias Lampakis 43.2(2012)174

Topic: Summation inequality involving a finite cyclic sequence

Solution: A lower bound on a sum 44.2(2013)144

973

Proposer: Ion Pătrașcu & Florentine Smarandache 43.2(2012)174

Topic: Identity for the sides of a triangle which is inscribed & circumscribed to circles

Solution: A condition for being a harmonic mean 44.2(2013)144

974

Proposer: Michael Woltermann 43.2(2012)175

Topic: Trigonometric identity involving cosines and inverse cosines

Solution: An expression for  $\cos(2\pi/7)$  44.2(2013)146

Proposer: Cezar Lupu 43.2(2012)175

Topic: Common point involving the orthocenters and centroids of triangles inside a hexagon

Solution: Cyclic hexagons, orthocenters and centroids 44.2(2013)147

976

Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanicu 43.3(2012)257

Topic: Inequality involving the semiperimeter, inradius and circumradius of a triangle

Solution: An inequality with a triangle 44.3(2013)234

977

Proposer: Greg Oman 43.3(2012)257

Topic: Proving a property involving subsets which are closed under a given function

Solution: Functions and Countable Sets 44.3(2013)235

978

Proposer: Michel Bataille 43.3(2012)257

Topic: Limits involving the n<sup>th</sup> harmonic number

Solution: A limit with harmonic numbers 44.3(2013)235

979

Proposer: Steven Finch 43.3(2012)258

Topic: Chordal triangle formed from points on a sphere and the probability that it is acute

Solution: The probability of an acute chordal triangle 44.3(2013)237

980

Proposer: George Apostolopoulos 43.3(2012)258

Topic: Finding the angles of a triangle formed from points on a square

Solution: Minimum area of a triangle andits angles 44.3(2013)238

981

Proposer: Michael Bataille 43.4(2012)337

Topic: Inequality involving the inradius and the smallest and largest sides of a triangle

Solution: Largest constant for an inequality of a triangle 44.4(2013)326

982

Proposer: Elias Lampakis 43.4(2012)337

Topic: Inequality involving the orthocenter, the circumradius and altitudes of a triangle

Solution: an inequality in a triangle 44.4(2013)327

983

Proposer: George Apostolopoulous 43.4(2012)337

Topic: Finding triangles of equal area constructed inside a give triangle Solution: A condition for triangles to hav equal area 44.4(2013)327

984

Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanicu 43.4(2012)338

Topic: Inequality involving sums of logarithms

Solution: a logarithmic function inequality 44.4(2013)330

Proposer: Greg Oman 43.4(2012)338

Topic: Proving that a certain infinite commutative ring is a principal ideal domain

Solution: Conditions for a principal ideal domain 44.4(2013)331

986

Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanicu 43.5(2012)410

Topic: Inequalities involving sines and cosines of the angles of an acute triangle

Solution: Inequalities with the sine and cosine functions 44.5(2013)438

987

Proposer: Ovidia Furdui 43.5(2012)410

Topic: Limit of the nth root of an integral involving logarithmic and exponential functions

Solution: A limit converging to 1/e 44.5(2013)440

988

Proposer: José Luis Díaz-Barrero 43.5(2012)410

Topic: Inequality involving a set of nonzero real numbers

Solution: Applications of Radon and Bergstrom inequalities 44.5(2013)441

989

Proposer: Yagub N. Aliyev 43.5(2012)411

Topic: Inequalities involving distances from vertices to points on the sides of a triangle

Solution: Inequality for areas of triangles 44.5(2013)442

990

Proposer: Ion Cucurezeanu & Cezar Lupu 43.5(2012)411

Topic: Limit involving the integral of a continuous real valued function on [-1,1]

Solution: A limit with the number of perfect squares 44.5(2013)444

991

Proposer: Ovidu Furdui 44.1(2013)65

Topic: Limits relating to a given sequence

Solution: The limits of two sequencesec 45.1(2014)58

992

Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanciu 44.1(2013)65

Topic: Sums relating to the inscribed and circumscribed circles of a polygon

Solution: An inequality fo a regular polygon 45.1(2014)60

993

Proposer: Michael Woltermann 44.1(2013)66

Topic: Establishing an inequality for the integral of a continuous function

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Topic: Inequality involving three variables and three constants whose product is one

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Proposer: Valery Karachik 44.4(2013)326

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Solution: Coaxal family determined by two circles 45.5(2014)398

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Proposer: Michel Bataille 46.3(2015)220

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Proposer: Ovidiu Furdui 46.3(2015)220

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Proposer: Stan Byrd & Roger Nichols 46.4(2015)300

Topic: Find the coefficients which minimize a definite integral of a cubic polnomial

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Proposer: Spiro P. Andriopoulos 46.4(2015)300

Topic: Inequality involving sums of two converging sequences of integers and their limits

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Topic: Inequality involving the sines of the angles of a triangle

Solution: An inequality involving sines 47.4(2016)304

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Proposer: George Apostolopoulos 46.4(2015)301

Topic: Inequality involving cosines, circumradius, inradius and semiperimeter of a triangle

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Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanicu 46.5(2015)369

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Proposer: Mircea Merca 46.5(2015)370; 47.2(2016)138

Topic: Inequality for a sum of cosines of a rational expression involving positive integers

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Proposer: Greg Oman 47.1(2016)61

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Solution: Artinian rings 48.1(2017)60

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Proposer: Spiros P.Andriopoulos 47.1(2016)61

Topic: Inequality involving a product of integrals of ratios of continuous positive functions

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Proposer: Ángel Plaza 47.1(2016)61

Topic: Finding the limit of a recursive sequence in terms of its initial conditions

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Proposer: Stephen Kaczkowski 47.1(2016)62

Topic: Find a closed form of the limit of a sequence involving the sum of powers of a ratio

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Proposer: Xiang Qian Chang 47.2(2016)138

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Proposer: Spiros P.Andriopoulos 47.2(2016)139

Topic: Inequality for the sum of a ratio involving powers of three positive numbers

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Proposer: George Apostolopoulos 47.2(2016)139

Topic: Formula for the tangent of the acute angle of the diagonals of a quadrilateral

Solution: Convex quadrilaterals 48.2(2017)142

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Proposer: Panagiote Ligouras 47.2(2016)139

Topic: Two inequalities for expression involving six positive real numbers

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Topic: Inequality for sums of expressions involving the sides of a triangle

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Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanicu 47.3(2016)221 Topic: Inequality involving the sides and circumradius of a triangle

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Proposer: Spiros P.Andriopoulos 47.3(2016)221

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Proposer: Valeriy Karachic & Leonid Menikhes 47.3(2016)222

Topic: Find and prove the limit for the fractional part of a sum of square roots

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Proposer: George Apostolopoulos 47.3(2016)222

Topic: Five inequalities of expressions involving three positive numbers whose sum is three

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Proposer: Michel Bataille 47.4(2016)300

Topic: Finding three numbers that relate to the definite integral of a ratio of polynomials

Solution: A limit of an integral 48.4(2017)293

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Proposer: Michael Goldenberg & Mark Kaplan 47.4(2016)300

Topic: Three conjectures involving a hyperbola related to a certain triangle

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Topic: Find the sum of a ratio of polynomials of integers Solution: A difference of familiar sums 48.4(2017)296

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Proposer: George Apostolopoulos 47.4(2016)301

Topic: Finding the maximum area of a certain triangle Solution: Maximizing the area of a triangle 48.4(2017)297

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Topic: Two conjectures involving quadruples of numbers relating to area in a quadrilateral

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Proposer: Michel Bataille 47.5(2016)369

Topic: Constructing a triangle with conditions on its legs with a set square

Solution: A triangle construction 48.5(2017)371

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Proposer: Ángel Plaza 47.5(2016)370

Topic: Proving a string of inequalities in three variables

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Proposer: Ovidiu Furdui 47.5(2016)370

Topic: Solving a functional equation in two variables

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Topic: Condition needed to prove that the sine of a 2x2 integral matrix is an integral matrix

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Topic: Proving the existence of a certain linearly independent subset in a vector space

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Proposer: Mehtaab Sawhney 48.1(2017)59

Topic: Finding quadratic polynomials in powers of a 2x2 matrix of quadratic polynomials

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Topic: Proving or disproving a statement about countable subsets closed under a function

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Topic: Consider the existence of a countable collection of ideals in a polynomial ring

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Topic: Proving the existence of a pseud-order on a finite field lacking transitivity

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Topic: Finding groups with two generating sets with nonempty intersection

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Topic: Inequality involving a finite polynomial sum with combinatoric coefficients

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Proposer: Francisco Javier Garcia Capitán 48.4(2017)292

Topic: Geometry problem involving a triangle and its circle of Apollonius

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Topic: Max-min problems involving square matrices

Solution: Bounds on the rank of a sum of matrices 49.4(2018)298

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Topic: Inequality involving a sequence whose limit is given

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Proposer: Greg Oman 48.5(2017)370

Topic: Finding a subsequence with an irrational sum from a given convergent sequence

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Proposer: Ovidiu Furdui 48.5(2017)370

Topic: Proving properties of a two by two matrix and the cosh of it

Solution: The hyperbolic cosine of a matrix 49.5(2018)373

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Proposer: Ovidiu Furdui 48.5(2017)371

Topic: Finding the limit of the n<sup>th</sup> power of a two by two matrix

Solution: Limit of powers of a matrix 49.5(2018)374

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Proposer: George Stoica 49.2(2018)140

Topic: Finite sum of even powers of a cosine function

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Proposer: D. M. Bătinetu-Giurgiu & Neculai Stanicu 49.3(2018)222

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Proposer: Paul Bracken 49.4(2018)295

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Proposer: Lirk Madsen 49.4(2018)295

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Topic: Prove or disprove the existence of a certain noncommutative ring

Solution: An infinite noncommutative ring all of whose proper unital subrings are commutative

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Topic: Prove that a multiplicative group with commutator and conditions is abelian Solution: A condition on comutators that implies a group is abelian 50.5(2019)380

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Solution: The limit of a sequence involving sines 50.5(2019)381

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Topic: Prove that a finite commutative ring with condition is a principal ideal ring

Solution: A condition for a ring to be a principal ideal ring 50.5(2019)381

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Topic: Prove that an integral involving powers of a logarithm yields the Riemann zeta function

and find the sum of a series involving Stirling numbers of the first kind

Solution: A sum involving Stirling numbers 50.5(2019)382

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left and right neighbors

Solution: Uncountable ordinals 50.5(2019)384

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Proposer: George Stoica 50.1(2019)61

Topic: Finding the number of roots of a certain polynomial

Solution: Real roots of a polynomial 51.1(2020)67

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Proposer: Ovidu Furdui & Alina Síntămărian 50.1(2019)61

Topic: Evaluate the limit of an integral involving powers of sines and cosines

Solution: Wallis integrals and the squeeze theorem to calculate the limit of an integral

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Topic: Prove that the lim sup of a ratio of logarithms is one

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Topic: Necessary and sufficient conditions concerning parallel lines in a scalene triangle

Solution: Co-linear points and parallel lines 51.1(2020)70

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Topic: Investigating some properties of a direct product of groups

Solution: When does an isomorphic product of groups imply isomorphic groups 51.1(2020)72

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Proposer: John Engbers & Adam Hammett George Stoica 50.2(2019)143

Topic: Finite summation identity involving Stirling numbers of the second kind Solution: An identity involving Stirling numbers of the second kind 51.2(2020)147

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Proposer: Souvik Dey 50.2(2019)143

Topic: Open subsets in a path connected T<sub>1</sub> topological space

Solution: Path connected T<sub>1</sub> spaces 51.2(2020)148

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Topic: Finding and proving the number of points inside a tetrahedron Solution: Integer lattice points in and on a tetrahedron 51.2(2020)148

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Proposer: George Stoica 50.2(2019)144

Topic: Equation involving sums containing combinatorial numbers and their reciprocals

Solution: A binomial sum identity 51.2(2020)149

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Proposer: Greg Oman 50.2(2019)144

Topic: Rings of sequences of real numbers

Solution: Non-isomorphic rings of infinite sequences 51.2(2020)151

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Proposer: Gregory Dresden 50.3(2019)224

Topic: Finding the highest power of 2 that divides any entry in powers of a 2x2 matrix

Solution: Highest power of two dividing an entry of a matrix 51.3(2020)227

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Topic: Inequality involving the area and circumradius of a triangle Solution: An inequality for the area of a triangle 51.3(2020)228

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Proposer: Eugen Ionascu 50.3(2019)224

Topic: Probability involving equally spaced points on a line segment

Solution: Probability of equally spaced points 51.3(2020)229

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Topic: Finding the value of derivatives of a product of sine functions for argument zero

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approach a limit of one

Solution: Convergent or divergent? 51.4(2020)307

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Topic: Convergence comparison test for a sum of terms of a sequence and the sum of a ratio

between members of the sequence and its partial sums

Solution: If the sum of terms divided by the partial sums converges, then so does the sum of terms

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Solution: An arctan inequality 51.4(2020)311

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Topic: Show given comparison of two quadrilaterals exist if and only if they are parallelograms

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Topic: Investigating the existence of an integral domain integral over a given integral domain Solution: An infinite integral domain has the same cardinality as the set of units of an integral

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Solution: {See Problem 1163} An integral equation 51.5(2020)388; 52.3(2021)230

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Topic: Inequalities involving the radius of the circumcircle of a triangle

Solution: Circles internally tangent to two sides of a triangle and the circumcircle 52.3(2021)230

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Topic: Show a necessary and sufficient condition that the triangle formed by a point on one of

the sides of an isosceles triangle, it's incenter and circumcenter form an equilateral

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Solution: A condition causing a prime ring to be commutative 53.3(2022)244

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Topic: Summation problem involving the product of triangle, harmonic and Fibonacci numbers

Solution: Harmonic, Fibonacci and triangular numbers 53.4(2022)320

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Proposer: Ovidiu Furdui & Alina Sîntămărian 52.4(2021)396

Topic: Proving a triple summation yields two Riemann zeta functions

Solution: A sum of products of sums 53.4(2022)321

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Topic: Proving an integral involving a product of logarithm functions yields a zeta function Solution: No solution will appear as the problem appeared in the May 2021 issue of the Monthly.

Solution: However: An integral of logarithms 53.4(2022)323

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Topic: Determining the existence of a certain integral domain and a special collection of ideals Solution: The existence of a countable commutative integral domain with a sum-free collection of

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Topic: Problem involving tiling asquare with rectangles

Solution: Tiling a square with small squares and narrow rectangles 54.2(2023)148

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Topic: Prove the existence of a function, f(x) satisfying an integral equation; and express it in

terms of elementary and that  $f^{k}(0)$  is related to Fibonacci numbers

Solution: Fibonacci numbers from the solution to an integral equation 54.2(2023)150

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Solution: Pell numbers and Pell-Lucas numbers 54.2(2023)152

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Solution: A criterion for a commutative ring to be a field 54.2(2023)153

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Solution: Cofactors of cofactors 54.2(2023)154

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Solution: Area of a polar graph 54.2(2023)154

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Solution: Which rectangular numbers are squares - again? 54.2(2023)158

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Topic: Proving that a certain finite group is cyclic

Solution: A criterion for a group to be cyclic 54.2(2023)159

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Topic: Two problems involving chained rings

Solution: A reduced ring with all subrings chained is a field 54.2(2023)159

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Topic: Inequality with three variables involving a logarithm

Solution: An easy logarithmic inequality 54.3(2003)238, 4.4(2023)395

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Solution: Primitive Heronian triangles with equivalent rectangles 54.3(2003)241, 54.4(2023)398

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Topic: Problem involving Catalan numbers and complex polynomials

Solution: The Catalan numbers 54.4(2023)401

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Topic: Prove two random variable are uniform over [0,1]

Solution: Uniform random variables 54.4(2023)402

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Topic: Finding the limit of a difference of two sums of inverse powers of integers Solution: The limit of a quotient of sequences defined by sums 54.4(2023)403

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Proposer: Greg Oman 53.4(2022)320

Topic: Finding structures of a Set and a function where the set is not finitely generated

Solution: Non-finitely generated sets whose proper subsets closed under a given function are all

finitely generated 54.4(2023)404

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Topic: Finding the centroid of special tetrahedron Solution: The centroid of a tetraghedron 54.5(2023)493

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Solution: Fields for which the collection of additive subgroups and the collection of multiplicative

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Topic: Inequality involving nth roots of sums of members of a sequence between 0 and 1

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Topic: Transcendental equation involving the arcsine and exponential functions

Solution: \*\*\*\*\*

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Proposer: Cezar Lupu 54.1(2023)70

Topic: Inequality involving the square of an integrable function

Solution: \*\*\*\*\*

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Proposer: Albert Natian 54.1(2023)71

Topic: Prove that the fractional part of a random variable is uniformly distributed over [0,1]

Solution: \*\*\*\*\*

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Proposer: George stoica 54.1(2023)71

Topic: Proving that a polynomial involving two sequences has real roots

Solution: \*\*\*\*\*

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Proposer: Cezar Lupu 54.2(2023)147

Topic: Inequality involving the square of an integrable function

Solution: \*\*\*\*\*

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Proposer: Moubinool Omarjee 54.2(2023)147

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Solution: \*\*\*\*\*

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Proposer: Greg Oman 54.2(2023)147

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Solution: \*\*\*\*\*

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Topic: Prove that the sum of products of a given sequence is a binomial number

Solution: \*\*\*\*\*

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Topic: Showing three properties of the determinant of a matrix with complex entries

Solution: \*\*\*\*\*

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Topic: Proving a factor of a sum of powers of a matrix

Solution: \*\*\*\*\*

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Topic: Showing na infinete sum involving a product of binomial expressions is  $1/\pi$ 

Solution: \*\*\*\*\*

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Proposer: Reza Farhadian 54.4(2023)394

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Solution: \*\*\*\*\*

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Proposer: Ovidiu Furdui & Alina Sîntămărian 54.4(2023)395

Topic: Finding the limit of an integral of the n<sup>th</sup> power of a binomial expression

Solution: \*\*\*\*\*

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Topic: Computing the expected value two minimal expressions

Solution: \*\*\*\*\*

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Topic: Finding fields and F-vector spaces with any two bases having non-empty intersections

Solution: \*\*\*\*\*

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Solution: \*\*\*\*\*

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Proposer: Alaric Pow Ian-Jun 54.4(2023)400

Topic: Identity involving the ratio of a sum of cosines over a sum of sines

Solution: \*\*\*\*\*

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Proposer: Antonio Garcia 54.4(2023)400

Topic: Inequality involving sums of products of roots involving three nonnegative numbers

Solution: \*\*\*\*\*

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Proposer: Nick Fiala & Greg Oman 54.4(2023)401

Topic: Proving that in finite negative poor division rings with more than 2 elements, all

elements have additive inverses

Solution: \*\*\*\*\*

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Topic: Infinite integral involving the arctangent function

Solution: \*\*\*\*\*

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Proposer: George Apostolopoulos 54.5(2023)492

Topic: Inequality involving the circumradius and the inradius of a triangle

Solution: \*\*\*\*\*

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Proposer: Marius Munteanu 54.5(2023)492

Topic: Find all solutions of a quintic polynomial equation with constant term between 0 and 1

Solution: \*\*\*\*\*

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Topic: Proving that a certain finite group of order at least 3 is abelian

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Topic: Double sum involving the Riemann zeta function

Solution: \*\*\*\*\*

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