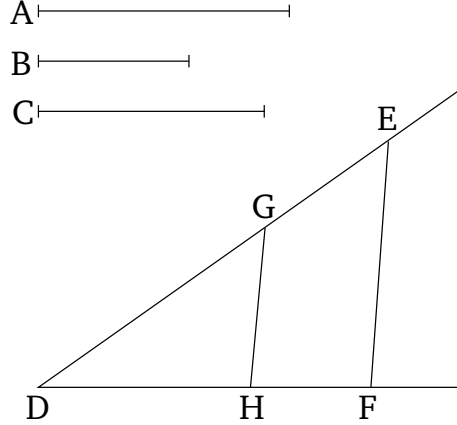


## Book 6

### Proposition 12

To find a fourth (straight-line) proportional to three given straight-lines.



Let  $A$ ,  $B$ , and  $C$  be the three given straight-lines. So it is required to find a fourth (straight-line) proportional to  $A$ ,  $B$ , and  $C$ .

Let the two straight-lines  $DE$  and  $DF$  be set out encompassing the [random] angle  $EDF$ . And let  $DG$  be made equal to  $A$ , and  $GE$  to  $B$ , and, further,  $DH$  to  $C$  [Prop. 1.3]. And  $GH$  being joined, let  $EF$  have been drawn through (point)  $E$  parallel to it [Prop. 1.31].

Therefore, since  $GH$  has been drawn parallel to one of the sides  $EF$  of triangle  $DEF$ , thus as  $DG$  is to  $GE$ , so  $DH$  (is) to  $HF$  [Prop. 6.2]. And  $DG$  (is) equal to  $A$ , and  $GE$  to  $B$ , and  $DH$  to  $C$ . Thus, as  $A$  is to  $B$ , so  $C$  (is) to  $HF$ .

Thus, a fourth (straight-line),  $HF$ , has been found (which is) proportional to the three given straight-lines,  $A$ ,  $B$ , and  $C$ . (Which is) the very thing it was required to do.