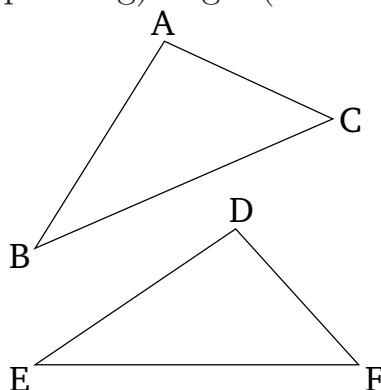


# Book 1

## Proposition 25

If two triangles have two sides equal to two sides, respectively, but (one) has a base greater than the base (of the other), then (the former triangle) will also have the angle encompassed by the equal straight-lines greater than the (corresponding) angle (in the latter).



Let  $ABC$  and  $DEF$  be two triangles having the two sides  $AB$  and  $AC$  equal to the two sides  $DE$  and  $DF$ , respectively (That is),  $AB$  (equal) to  $DE$ , and  $AC$  to  $DF$ . And let the base  $BC$  be greater than the base  $EF$ . I say that angle  $BAC$  is also greater than  $EDF$ .

For if not, ( $BAC$ ) is certainly either equal to, or less than, ( $EDF$ ). In fact,  $BAC$  is not equal to  $EDF$ . For then the base  $BC$  would also have been equal to the base  $EF$  [Prop. 1.4]. But it is not. Thus, angle  $BAC$  is not equal to  $EDF$ . Neither, indeed, is  $BAC$  less than  $EDF$ . For then the base  $BC$  would also have been less than the base  $EF$  [Prop. 1.24]. But it is not. Thus, angle  $BAC$  is not less than  $EDF$ . But it was shown that ( $BAC$ ) is not equal (to  $EDF$ ) either. Thus,  $BAC$  is greater than

*EDF.*

Thus, if two triangles have two sides equal to two sides, respectively, but (one) has a base greater than the base (of the other), then (the former triangle) will also have the angle encompassed by the equal straight-lines greater than the (corresponding) angle (in the latter). (Which is) the very thing it was required to show.