

# Book 5

## Proposition 7

Equal (magnitudes) have the same ratio to the same (magnitude), and the latter (magnitude has the same ratio) to the equal (magnitudes).

Let  $A$  and  $B$  be equal magnitudes, and  $C$  some other random magnitude. I say that  $A$  and  $B$  each have the same ratio to  $C$ , and (that)  $C$  (has the same ratio) to each of  $A$  and  $B$ .

For let the equal multiples  $D$  and  $E$  have been taken of  $A$  and  $B$  (respectively), and the other random multiple  $F$  of  $C$ .

Therefore, since  $D$  and  $E$  are equal multiples of  $A$  and  $B$  (respectively), and  $A$  (is) equal to  $B$ ,  $D$  (is) thus also equal to  $E$ . And  $F$  (is) different, at random. Thus, if  $D$  exceeds  $F$  then  $E$  also exceeds  $F$ , and if ( $D$  is) equal (to  $F$  then  $E$  is also) equal (to  $F$ ), and if ( $D$  is) less (than  $F$  then  $E$  is also) less (than  $F$ ). And  $D$  and  $E$  are equal multiples of  $A$  and  $B$  (respectively), and  $F$  another random multiple of  $C$ . Thus, as  $A$  (is) to  $C$ , so  $B$  (is) to  $C$  [Def. 5.5].

[So] I say that  $C$  also has the same ratio to each of  $A$  and  $B$ .

For, similarly, we can show, by the same construction, that  $D$  is equal to  $E$ . And  $F$  (has) some other (value). Thus, if  $F$  exceeds  $D$  then it also exceeds  $E$ , and if ( $F$  is) equal (to  $D$  then it is also) equal (to  $E$ ), and if ( $F$  is) less (than  $D$  then it is also) less (than  $E$ ). And  $F$  is a multiple of  $C$ , and  $D$  and  $E$  other random equal

multiples of  $A$  and  $B$ . Thus, as  $C$  (is) to  $A$ , so  $C$  (is) to  $B$  [Def. 5.5].

Thus, equal (magnitudes) have the same ratio to the same (magnitude), and the latter (magnitude has the same ratio) to the equal (magnitudes).

## Corollary

So (it is) clear, from this, that if some magnitudes are proportional then they will also be proportional inversely. (Which is) the very thing it was required to show.