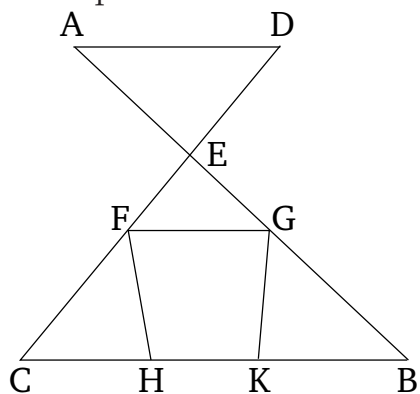


# Book 11

## Proposition 2

If two straight-lines cut one another then they are in one plane, and every triangle (formed using segments of both lines) is in one plane.



For let the two straight-lines  $AB$  and  $CD$  have cut one another at point  $E$ . I say that  $AB$  and  $CD$  are in one plane, and that every triangle (formed using segments of both lines) is in one plane.

For let the random points  $F$  and  $G$  have been taken on  $EC$  and  $EB$  (respectively). And let  $CB$  and  $FG$  have been joined, and let  $FH$  and  $GK$  have been drawn across. I say, first of all, that triangle  $ECB$  is in one (reference) plane. For if part of triangle  $ECB$ , either  $FHC$  or  $GBK$ , is in the reference [plane], and the remainder in a different (plane) then a part of one the straight-lines  $EC$  and  $EB$  will also be in the reference plane, and (a part) in a different (plane). And if the part  $FCBG$  of triangle  $ECB$  is in the reference plane, and the remainder in a different (plane) then parts of both of the straight-lines  $EC$  and  $EB$  will also be in the reference plane,

and (parts) in a different (plane). The very thing was shown to be absurd [Prop. 11.1]. Thus, triangle  $ECB$  is in one plane. And in whichever (plane) triangle  $ECB$  is (found), in that (plane)  $EC$  and  $EB$  (will) each also (be found). And in whichever (plane)  $EC$  and  $EB$  (are) each (found), in that (plane)  $AB$  and  $CD$  (will) also (be found) [Prop. 11.1]. Thus, the straight-lines  $AB$  and  $CD$  are in one plane, and every triangle (formed using segments of both lines) is in one plane. (Which is) the very thing it was required to show.