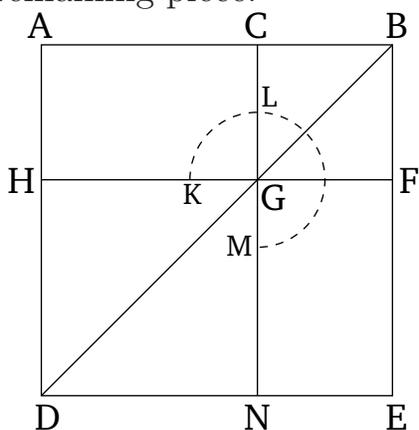


Book 2

Proposition 7

If a straight-line is cut at random then the sum of the squares on the whole (straight-line), and one of the pieces (of the straight-line), is equal to twice the rectangle contained by the whole, and the said piece, and the square on the remaining piece.



For let any straight-line AB have been cut, at random, at point C . I say that the (sum of the) squares on AB and BC is equal to twice the rectangle contained by AB and BC , and the square on CA .

For let the square $ADEB$ have been described on AB [Prop. 1.46], and let the (rest of) the figure have been drawn.

Therefore, since (rectangle) AG is equal to (rectangle) GE [Prop. 1.43], let the (square) CF have been added to both. Thus, the whole (rectangle) AF is equal to the whole (rectangle) CE . Thus, (rectangle) AF plus (rectangle) CE is double (rectangle) AF . But, (rectangle) AF plus (rectangle) CE is the gnomon KLM , and the square CF . Thus, the gnomon KLM , and the square

CF , is double the (rectangle) AF . But double the (rectangle) AF is also twice the (rectangle contained) by AB and BC . For BF (is) equal to BC . Thus, the gnomon KLM , and the square CF , are equal to twice the (rectangle contained) by AB and BC . Let DG , which is the square on AC , have been added to both. Thus, the gnomon KLM , and the squares BG and GD , are equal to twice the rectangle contained by AB and BC , and the square on AC . But, the gnomon KLM and the squares BG and GD is (equivalent to) the whole of $ADEB$ and CF , which are the squares on AB and BC (respectively). Thus, the (sum of the) squares on AB and BC is equal to twice the rectangle contained by AB and BC , and the square on AC .

Thus, if a straight-line is cut at random then the sum of the squares on the whole (straight-line), and one of the pieces (of the straight-line), is equal to twice the rectangle contained by the whole, and the said piece, and the square on the remaining piece. (Which is) the very thing it was required to show.