

## Book 3

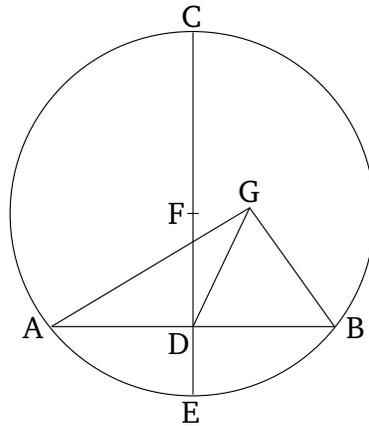
### Proposition 1

To find the center of a given circle.

Let  $ABC$  be the given circle. So it is required to find the center of circle  $ABC$ .

Let some straight-line  $AB$  have been drawn through  $(ABC)$ , at random, and let  $(AB)$  have been cut in half at point  $D$  [Prop. 1.9]. And let  $DC$  have been drawn from  $D$ , at right-angles to  $AB$  [Prop. 1.11]. And let  $(CD)$  have been drawn through to  $E$ . And let  $CE$  have been cut in half at  $F$  [Prop. 1.9]. I say that (point)  $F$  is the center of the [circle]  $ABC$ .

For (if) not then, if possible, let  $G$  (be the center of the circle), and let  $GA$ ,  $GD$ , and  $GB$  have been joined. And since  $AD$  is equal to  $DB$ , and  $DG$  (is) common, the two (straight-lines)  $AD$ ,  $DG$  are equal to the two (straight-lines)  $BD$ ,  $DG$ ,<sup>†</sup> respectively. And the base  $GA$  is equal to the base  $GB$ . For (they are both) radii. Thus, angle  $ADG$  is equal to angle  $GDB$  [Prop. 1.8]. And when a straight-line stood upon (another) straight-line make adjacent angles (which are) equal to one another, each of the equal angles is a right-angle [Def. 1.10]. Thus,  $GDB$  is a right-angle. And  $FDB$  is also a right-angle. Thus,  $FDB$  (is) equal to  $GDB$ , the greater to the lesser. The very thing is impossible. Thus, (point)  $G$  is not the center of the circle  $ABC$ . So, similarly, we can show that neither is any other (point) except  $F$ .



Thus, point  $F$  is the center of the [circle]  $ABC$ .

## Corollary

So, from this, (it is) manifest that if any straight-line in a circle cuts any (other) straight-line in half, and at right-angles, then the center of the circle is on the former (straight-line). — (Which is) the very thing it was required to do.