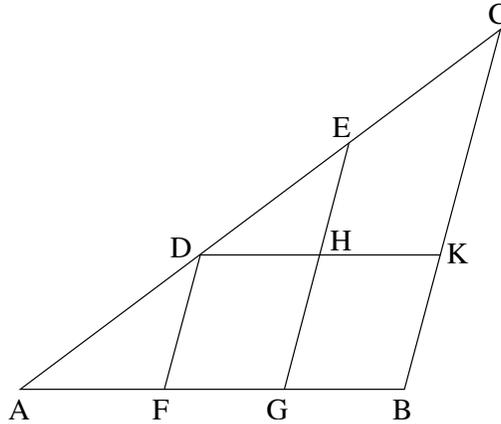


## Book 6 Proposition 10

To cut a given uncut straight-line similarly to a given cut (straight-line).



Let  $AB$  be the given uncut straight-line, and  $AC$  a (straight-line) cut at points  $D$  and  $E$ , and let  $(AC)$  be laid down so as to encompass a random angle (with  $AB$ ). And let  $CB$  have been joined. And let  $DF$  and  $EG$  have been drawn through (points)  $D$  and  $E$  (respectively), parallel to  $BC$ , and let  $DHK$  have been drawn through (point)  $D$ , parallel to  $AB$  [Prop. 1.31].

Thus,  $FH$  and  $HB$  are each parallelograms. Thus,  $DH$  (is) equal to  $FG$ , and  $HK$  to  $GB$  [Prop. 1.34]. And since the straight-line  $HE$  has been drawn parallel to one of the sides,  $KC$ , of triangle  $DKC$ , thus, proportionally, as  $CE$  is to  $ED$ , so  $KH$  (is) to  $HD$  [Prop. 6.2]. And  $KH$  (is) equal to  $BG$ , and  $HD$  to  $GF$ . Thus, as  $CE$  is to  $ED$ , so  $BG$  (is) to  $GF$ . Again, since  $FD$  has been drawn parallel to one of the sides,  $GE$ , of triangle  $AGE$ , thus, proportionally, as  $ED$  is to  $DA$ , so  $GF$  (is) to  $FA$  [Prop. 6.2]. And it was also shown that as  $CE$  (is) to

$ED$ , so  $BG$  (is) to  $GF$ . Thus, as  $CE$  is to  $ED$ , so  $BG$  (is) to  $GF$ , and as  $ED$  (is) to  $DA$ , so  $GF$  (is) to  $FA$ .

Thus, the given uncut straight-line,  $AB$ , has been cut similarly to the given cut straight-line,  $AC$ . (Which is) the very thing it was required to do.