

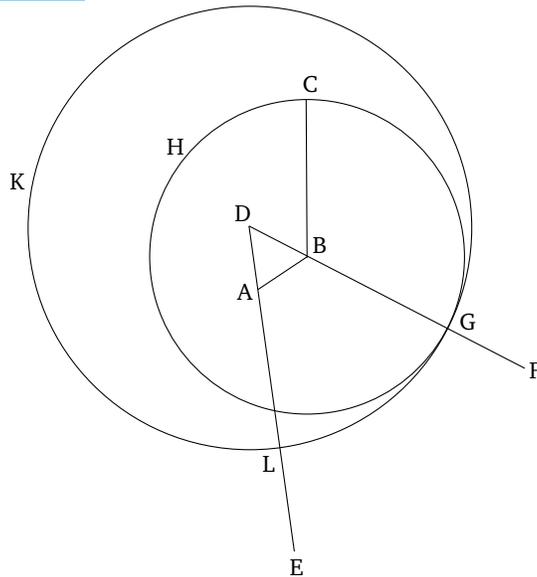
# Book 1

## Proposition 2

To place a straight-line equal to a given straight-line at a given point (as an extremity).

Let  $A$  be the given point, and  $BC$  the given straight-line. So it is required to place a straight-line at point  $A$  equal to the given straight-line  $BC$ .

For let the straight-line  $AB$  have been joined from point  $A$  to point  $B$  [Post. 1], and let the equilateral triangle  $DAB$  have been constructed upon it [Prop. 1.1]. And let the straight-lines  $AE$  and  $BF$  have been produced in a straight-line with  $DA$  and  $DB$  (respectively) [Post. 2]. And let the circle  $CGH$  with center  $B$  and radius  $BC$  have been drawn [Post. 3], and again let the circle  $GKL$  with center  $D$  and radius  $DG$  have been drawn [Post. 3].



Therefore, since the point  $B$  is the center of (the circle)

$CGH$ ,  $BC$  is equal to  $BG$  [Def. 1.15]. Again, since the point  $D$  is the center of the circle  $GKL$ ,  $DL$  is equal to  $DG$  [Def. 1.15]. And within these,  $DA$  is equal to  $DB$ . Thus, the remainder  $AL$  is equal to the remainder  $BG$  [C.N. 3]. But  $BC$  was also shown (to be) equal to  $BG$ . Thus,  $AL$  and  $BC$  are each equal to  $BG$ . But things equal to the same thing are also equal to one another [C.N. 1]. Thus,  $AL$  is also equal to  $BC$ .

Thus, the straight-line  $AL$ , equal to the given straight-line  $BC$ , has been placed at the given point  $A$ . (Which is) the very thing it was required to do.