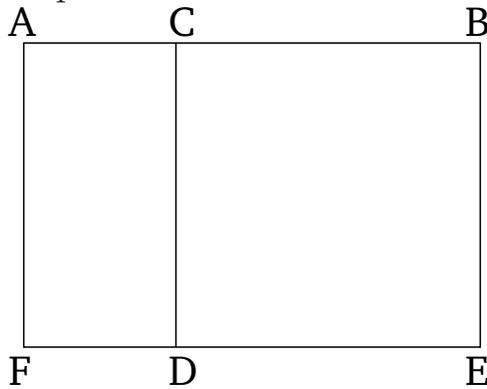


## Book 2

### Proposition 3

If a straight-line is cut at random then the rectangle contained by the whole (straight-line), and one of the pieces (of the straight-line), is equal to the rectangle contained by (both of) the pieces, and the square on the aforementioned piece.



For let the straight-line  $AB$  have been cut, at random, at (point)  $C$ . I say that the rectangle contained by  $AB$  and  $BC$  is equal to the rectangle contained by  $AC$  and  $CB$ , plus the square on  $BC$ .

For let the square  $CDEB$  have been described on  $CB$  [Prop. 1.46], and let  $ED$  have been drawn through to  $F$ , and let  $AF$  have been drawn through  $A$ , parallel to either of  $CD$  or  $BE$  [Prop. 1.31]. So the (rectangle)  $AE$  is equal to the (rectangle)  $AD$  and the (square)  $CE$ . And  $AE$  is the rectangle contained by  $AB$  and  $BC$ . For it is contained by  $AB$  and  $BE$ , and  $BE$  (is) equal to  $BC$ . And  $AD$  (is) the (rectangle contained) by  $AC$  and  $CB$ . For  $DC$  (is) equal to  $CB$ . And  $DB$  (is) the square on  $CB$ . Thus, the rectangle contained by  $AB$  and  $BC$  is equal to the rectangle contained by  $AC$  and  $CB$ , plus

the square on  $BC$ .

Thus, if a straight-line is cut at random then the rectangle contained by the whole (straight-line), and one of the pieces (of the straight-line), is equal to the rectangle contained by (both of) the pieces, and the square on the aforementioned piece. (Which is) the very thing it was required to show.