



shown in the theorem before this (one). And since  $D$  has made  $K$  (by) multiplying  $C$ , and has made  $M$  (by) multiplying  $F$ , thus as  $C$  is to  $F$ , so  $K$  (is) to  $M$  [Prop. 7.17]. But, as  $K$  (is) to  $M$ , (so)  $M$  (is) to  $L$ . Thus,  $K, M, L$  are continuously proportional in the ratio of  $C$  to  $F$ . And since as  $C$  is to  $D$ , so  $F$  (is) to  $G$ , thus, alternately, as  $C$  is to  $F$ , so  $D$  (is) to  $G$  [Prop. 7.13]. And so, for the same (reasons), as  $D$  (is) to  $G$ , so  $E$  (is) to  $H$ . Thus,  $K, M, L$  are continuously proportional in the ratio of  $C$  to  $F$ , and of  $D$  to  $G$ , and, further, of  $E$  to  $H$ . So let  $E, H$  make  $N, O$ , respectively, (by) multiplying  $M$ . And since  $A$  is solid, and  $C, D, E$  are its sides,  $E$  has thus made  $A$  (by) multiplying the (number created) from (multiplying)  $C, D$ . And  $K$  is the (number created) from (multiplying)  $C, D$ . Thus,  $E$  has made  $A$  (by) multiplying  $K$ . And so, for the same (reasons),  $H$  has made  $B$  (by) multiplying  $L$ . And since  $E$  has made  $A$  (by) multiplying  $K$ , but has, in fact, also made  $N$  (by) multiplying  $M$ , thus as  $K$  is to  $M$ , so  $A$  (is) to  $N$  [Prop. 7.17]. And as  $K$  (is) to  $M$ , so  $C$  (is) to  $F$ , and  $D$  to  $G$ , and, further,  $E$  to  $H$ . And thus as  $C$  (is) to  $F$ , and  $D$  to  $G$ , and  $E$  to  $H$ , so  $A$  (is) to  $N$ . Again, since  $E, H$  have made  $N, O$ , respectively, (by) multiplying  $M$ , thus as  $E$  is to  $H$ , so  $N$  (is) to  $O$  [Prop. 7.18]. But, as  $E$  (is) to  $H$ , so  $C$  (is) to  $F$ , and  $D$  to  $G$ . And thus as  $C$  (is) to  $F$ , and  $D$  to  $G$ , and  $E$  to  $H$ , so (is)  $A$  to  $N$ , and  $N$  to  $O$ . Again, since  $H$  has made  $O$  (by) multiplying  $M$ , but has, in fact, also made  $B$  (by) multiplying  $L$ , thus as  $M$  (is) to  $L$ , so  $O$  (is) to  $B$  [Prop. 7.17]. But, as  $M$  (is) to  $L$ , so  $C$  (is) to  $F$ , and  $D$  to  $G$ , and  $E$  to  $H$ . And thus as  $C$  (is) to  $F$ , and  $D$

to  $G$ , and  $E$  to  $H$ , so not only (is)  $O$  to  $B$ , but also  $A$  to  $N$ , and  $N$  to  $O$ . Thus,  $A$ ,  $N$ ,  $O$ ,  $B$  are continuously proportional in the aforementioned ratios of the sides.

So I say that  $A$  also has to  $B$  a cubed ratio with respect to (that) a corresponding side (has) to a corresponding side—that is to say, with respect to (that) the number  $C$  (has) to  $F$ , or  $D$  to  $G$ , and, further,  $E$  to  $H$ . For since  $A$ ,  $N$ ,  $O$ ,  $B$  are four continuously proportional numbers,  $A$  thus has to  $B$  a cubed ratio with respect to (that)  $A$  (has) to  $N$  [Def. 5.10]. But, as  $A$  (is) to  $N$ , so it was shown (is)  $C$  to  $F$ , and  $D$  to  $G$ , and, further,  $E$  to  $H$ . And thus  $A$  has to  $B$  a cubed ratio with respect to (that) a corresponding side (has) to a corresponding side—that is to say, with respect to (that) the number  $C$  (has) to  $F$ , and  $D$  to  $G$ , and, further,  $E$  to  $H$ . (Which is) the very thing it was required to show.