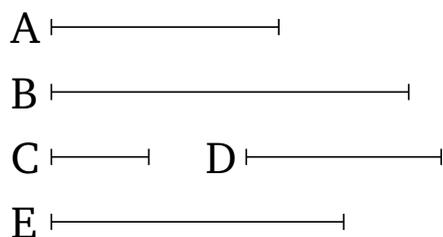


## Book 8

### Proposition 11

There exists one number in mean proportion to two (given) square numbers.<sup>†</sup> And (one) square (number) has to the (other) square (number) a squared<sup>‡</sup> ratio with respect to (that) the side (of the former has) to the side (of the latter).



Let  $A$  and  $B$  be square numbers, and let  $C$  be the side of  $A$ , and  $D$  (the side) of  $B$ . I say that there exists one number in mean proportion to  $A$  and  $B$ , and that  $A$  has to  $B$  a squared ratio with respect to (that)  $C$  (has) to  $D$ .

For let  $C$  make  $E$  (by) multiplying  $D$ . And since  $A$  is square, and  $C$  is its side,  $C$  has thus made  $A$  (by) multiplying itself. And so, for the same (reasons),  $D$  has made  $B$  (by) multiplying itself. Therefore, since  $C$  has made  $A$ ,  $E$  (by) multiplying  $C$ ,  $D$ , respectively, thus as  $C$  is to  $D$ , so  $A$  (is) to  $E$  [Prop. 7.17]. And so, for the same (reasons), as  $C$  (is) to  $D$ , so  $E$  (is) to  $B$  [Prop. 7.18]. And thus as  $A$  (is) to  $E$ , so  $E$  (is) to  $B$ . Thus, one number (namely,  $E$ ) is in mean proportion to  $A$  and  $B$ .

So I say that  $A$  also has to  $B$  a squared ratio with respect to (that)  $C$  (has) to  $D$ . For since  $A$ ,  $E$ ,  $B$  are three (continuously) proportional numbers,  $A$  thus has to  $B$  a squared ratio with respect to (that)  $A$  (has) to  $E$

[Def. 5.9]. And as  $A$  (is) to  $E$ , so  $C$  (is) to  $D$ . Thus,  $A$  has to  $B$  a squared ratio with respect to (that) side  $C$  (has) to (side)  $D$ . (Which is) the very thing it was required to show.