

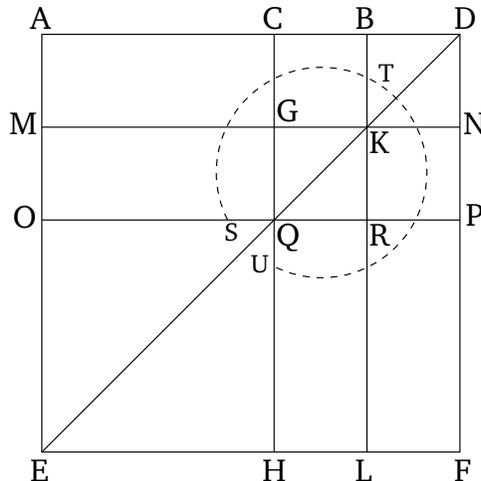
Book 2

Proposition 8

If a straight-line is cut at random then four times the rectangle contained by the whole (straight-line), and one of the pieces (of the straight-line), plus the square on the remaining piece, is equal to the square described on the whole and the former piece, as on one (complete straight-line).

For let any straight-line AB have been cut, at random, at point C . I say that four times the rectangle contained by AB and BC , plus the square on AC , is equal to the square described on AB and BC , as on one (complete straight-line).

For let BD have been produced in a straight-line [with the straight-line AB], and let BD be made equal to CB [Prop. 1.3], and let the square $AEFD$ have been described on AD [Prop. 1.46], and let the (rest of the) figure have been drawn double.



Therefore, since CB is equal to BD , but CB is equal

to GK [Prop. 1.34], and BD to KN [Prop. 1.34], GK is thus also equal to KN . So, for the same (reasons), QR is equal to RP . And since BC is equal to BD , and GK to KN , (square) CK is thus also equal to (square) KD , and (square) GR to (square) RN [Prop. 1.36]. But, (square) CK is equal to (square) RN . For (they are) complements in the parallelogram CP [Prop. 1.43]. Thus, (square) KD is also equal to (square) GR . Thus, the four (squares) DK , CK , GR , and RN are equal to one another. Thus, the four (taken together) are quadruple (square) CK . Again, since CB is equal to BD , but BD (is) equal to BK —that is to say, CG —and CB is equal to GK —that is to say, GQ — CG is thus also equal to GQ . And since CG is equal to GQ , and QR to RP , (rectangle) AG is also equal to (rectangle) MQ , and (rectangle) QL to (rectangle) RF [Prop. 1.36]. But, (rectangle) MQ is equal to (rectangle) QL . For (they are) complements in the parallelogram ML [Prop. 1.43]. Thus, (rectangle) AG is also equal to (rectangle) RF . Thus, the four (rectangles) AG , MQ , QL , and RF are equal to one another. Thus, the four (taken together) are quadruple (rectangle) AG . And it was also shown that the four (squares) CK , KD , GR , and RN (taken together are) quadruple (square) CK . Thus, the eight (figures taken together), which comprise the gnomon STU , are quadruple (rectangle) AK . And since AK is the (rectangle contained) by AB and BD , for BK (is) equal to BD , four times the (rectangle contained) by AB and BD is quadruple (rectangle) AK . But the gnomon STU was also shown (to be equal to) quadruple (rectangle)

AK. Thus, four times the (rectangle contained) by *AB* and *BD* is equal to the gnomon *STU*. Let *OH*, which is equal to the square on *AC*, have been added to both. Thus, four times the rectangle contained by *AB* and *BD*, plus the square on *AC*, is equal to the gnomon *STU*, and the (square) *OH*. But, the gnomon *STU* and the (square) *OH* is (equivalent to) the whole square *AEFD*, which is on *AD*. Thus, four times the (rectangle contained) by *AB* and *BD*, plus the (square) on *AC*, is equal to the square on *AD*. And *BD* (is) equal to *BC*. Thus, four times the rectangle contained by *AB* and *BC*, plus the square on *AC*, is equal to the (square) on *AD*, that is to say the square described on *AB* and *BC*, as on one (complete straight-line).

Thus, if a straight-line is cut at random then four times the rectangle contained by the whole (straight-line), and one of the pieces (of the straight-line), plus the square on the remaining piece, is equal to the square described on the whole and the former piece, as on one (complete straight-line). (Which is) the very thing it was required to show.